

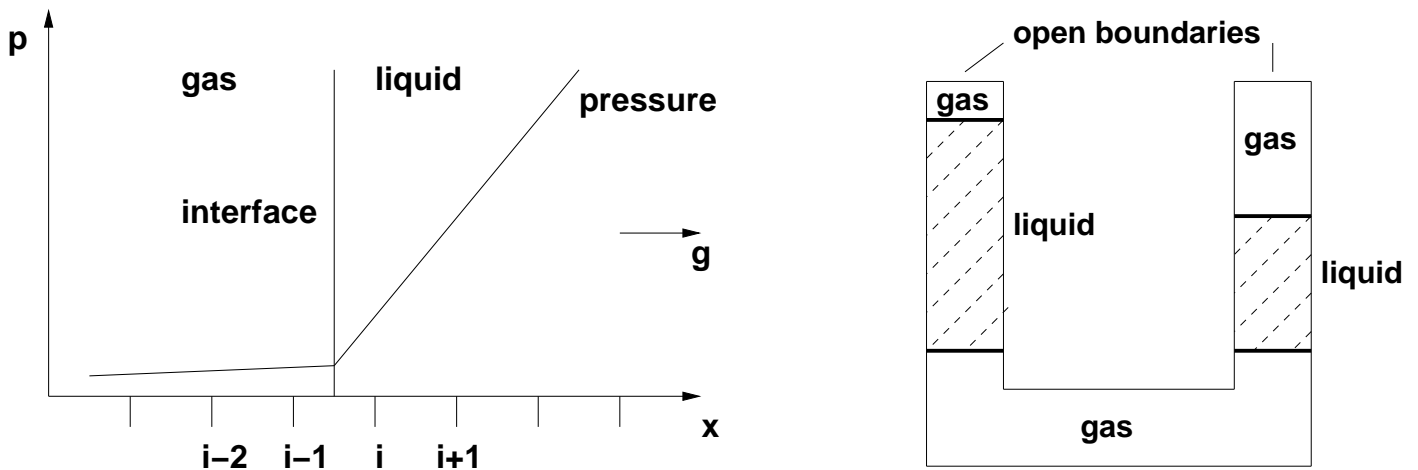
VIOLENT FREE SURFACE MOTION: EXAMPLES

- Wave Breaking
 - Shores
 - Ships
- Extreme Wave-Structure Interactions
 - Sloshing
 - Slamming
 - Green Water on Deck
 - Offshore Platforms

VIOLENT FREE SURFACE MOTION: OPTIONS

- Interface Tracking
 - Move Mesh With Free Surface
 - Free Surface = Boundary of Domain
 - Problems When Topology Changes
(e.g. Wave Breaking)
- Interface Capturing
 - Gas/Water Both Treated
 - Free Surface 'Captured' in Domain
 - Allows for Arbitrary Topology
 - Not as Accurate

INTERFACE CAPTURING: MODEL PROBLEMS



Hydrostatic Pressure Distribution and Communicating Tubes

- Consider Air:
 - Discontinuity in Pressure Gradient
 - \Rightarrow Spurious Air Acceleration
 - \Rightarrow Neglect Air
- Neglect Air:
 - Air Pocket Can Not Push on Water

DESCRIPTION OF INTERFACE

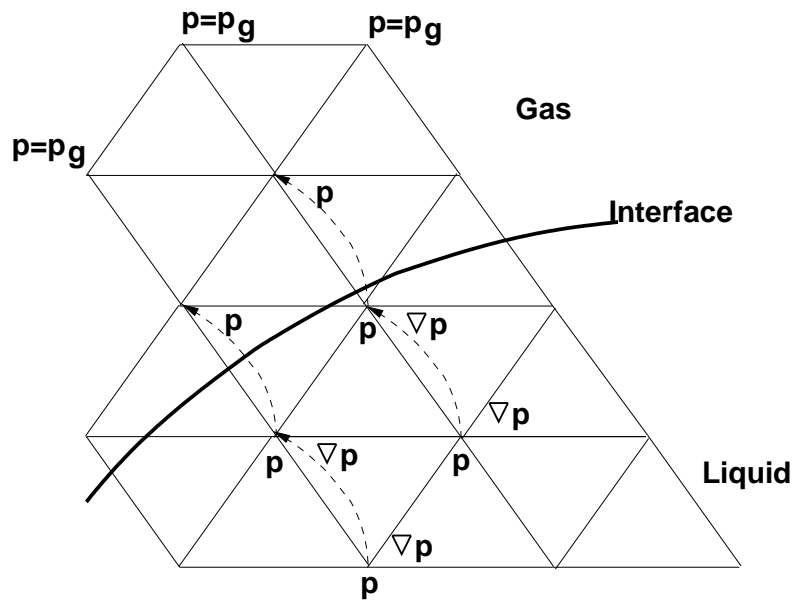
Liquid-Gas Interface:

$$\Phi_{,t} + \mathbf{v}_a \cdot \nabla \Phi = 0$$

Interpretations of Φ :

- Volume of Fluid (VOF): Density of Material (Nichols'75, Hirt'81, Many Others...)
- Pseudo-Concentration (PC): Percentage of Liquid
- Level Set (LS): Signed Distance to Interface (Osher, Fedkiw, Many Others...)

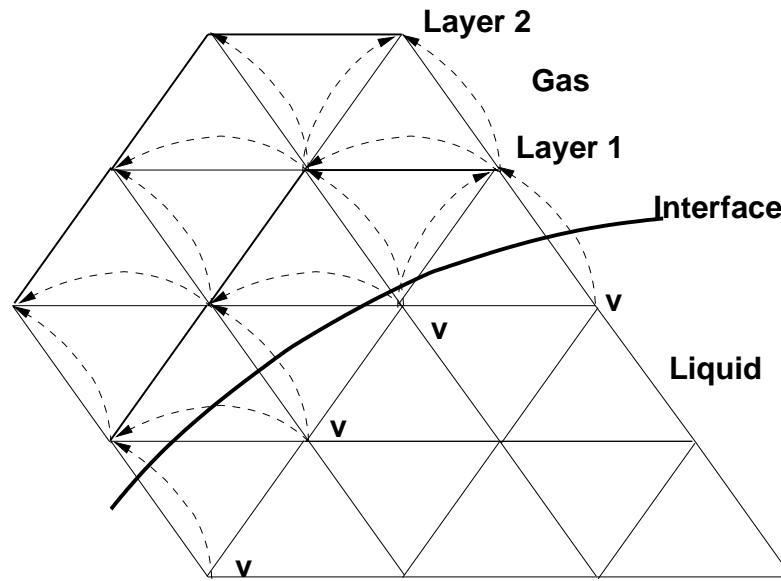
PRESSURE EXTRAPOLATION



Extrapolation of the Pressure

1. Set p_{gas} to Atmospheric/Bubble Value
2. Obtain ∇p Close to Interface
3. Extrapolate ∇p to Interface Points
4. Obtain Pressures in Gas Region

VELOCITY EXTRAPOLATION



Extrapolation of the Velocity

1. Set $\mathbf{v}_{gas} = 0$
2. Extrapolate \mathbf{v} From Liquid to Gas [Layers]

IMPOSITION OF CONSTANT MASS

Observation: Mass Not Constant (Small, But Significant)

- At the End of Each Timestep:
Restore by Adding/Removing
- Make Proportional to Interface Velocity

$$v_n = \left| \mathbf{v} \cdot \frac{\nabla \Phi}{|\nabla \Phi|} \right|$$

- Convergence Usually Very Fast (2-3 Iterations)

DEACTIVATION OF AIR REGION

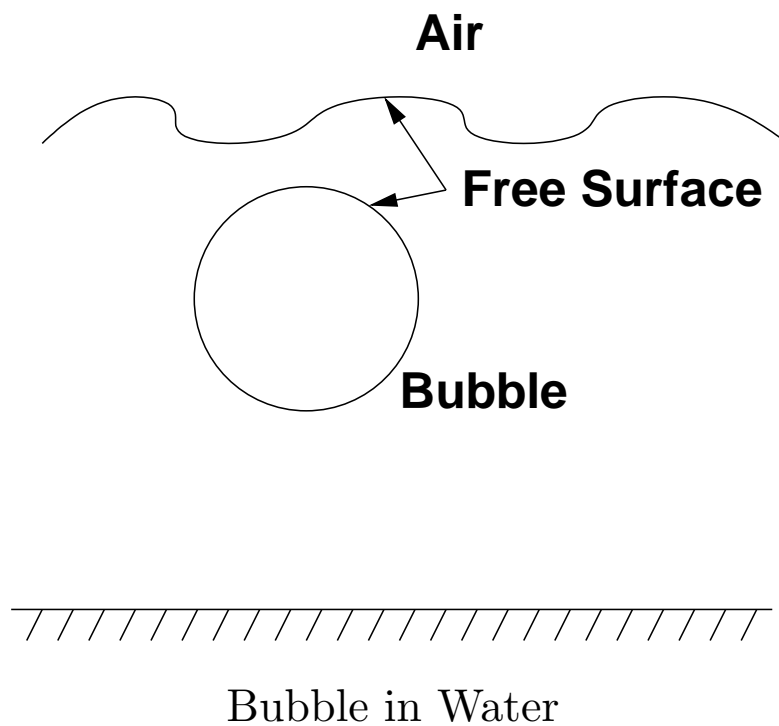
Air Region Not Updated \Rightarrow Avoid Work

- Mark/Deactivate Edge-Groups in Air Region

TREATMENT OF BUBBLES (1)

Assumption: Pressure in Bubble Constant

- Timescales
 - Speed of Sound/Bubble Size (1/100 sec)
 - Bubble Growth/Collapse (1 sec)



TREATMENT OF BUBBLES (2)

Isentropic Gas:

$$\frac{p_b}{p_{b0}} = \left(\frac{\rho_b}{\rho_{b0}} \right)^\gamma$$

Bubble ‘Marker’ Equation:

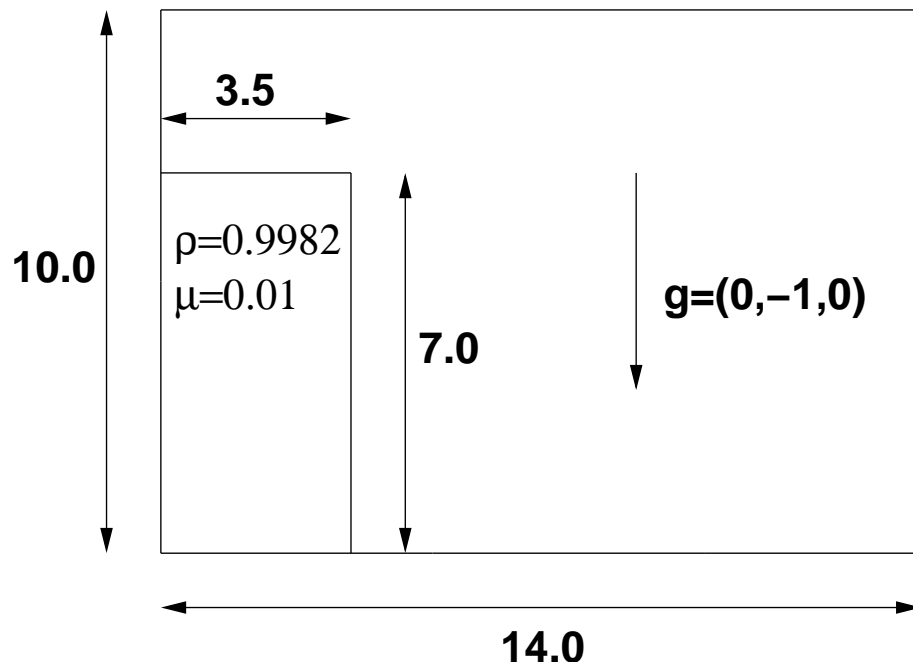
$$b_{,t} + \mathbf{v}_a \cdot \nabla b = 0$$

If Bubble Contacts Air: Extend Volume $\Rightarrow p \rightarrow 0$

VOF TIMESTEP

- If Required: Update Bubble Pressure
- Extrapolate Pressure
- Predict Velocity
- Update Pressure
- Correct Velocity ($\nabla \cdot \mathbf{v} = 0$)
- Extrapolate Velocity Field
- Update Scalar Interface Indicator
- Enforce Mass Conservation

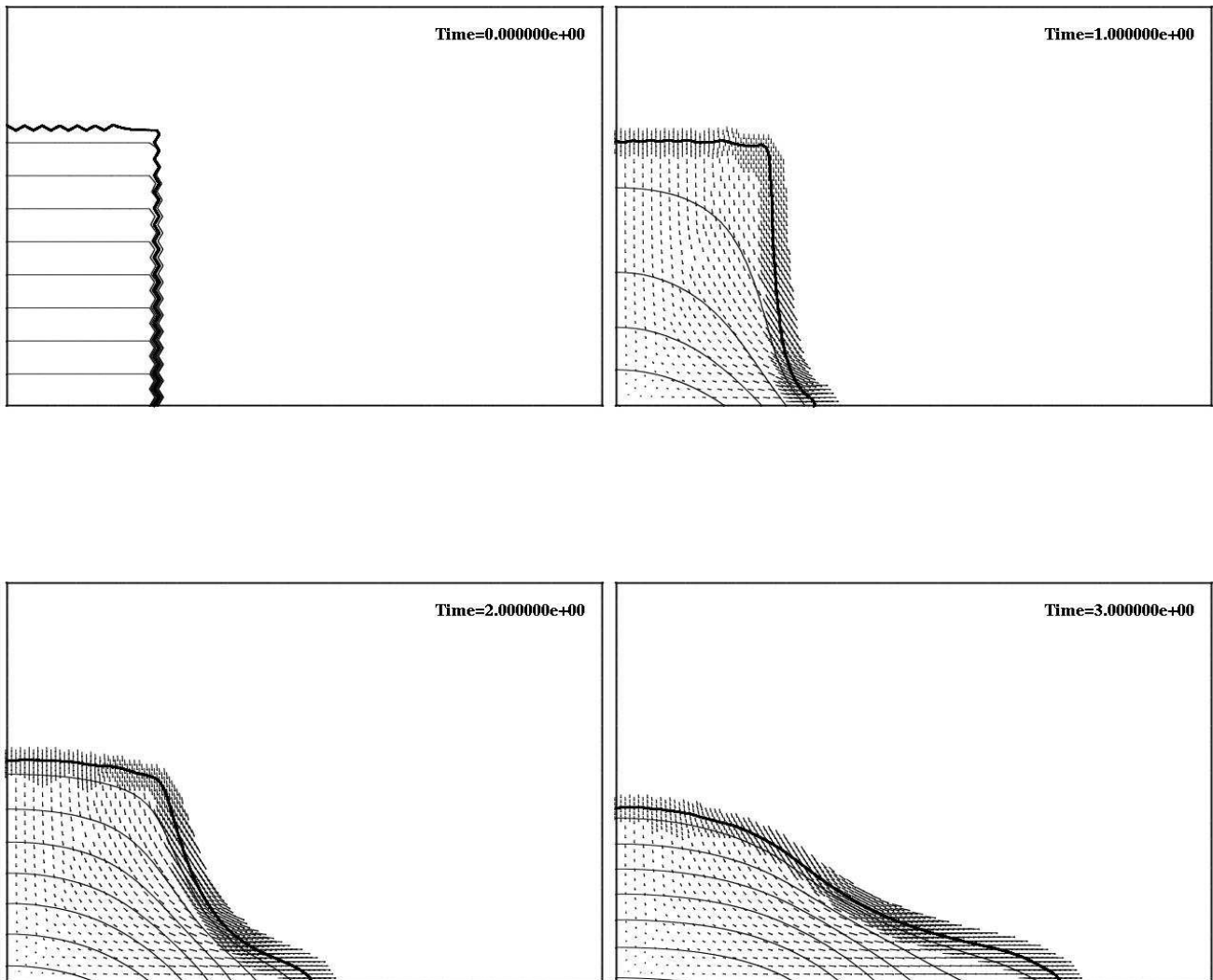
BREAKING DAM (1)



Breaking Dam: Problem Definition

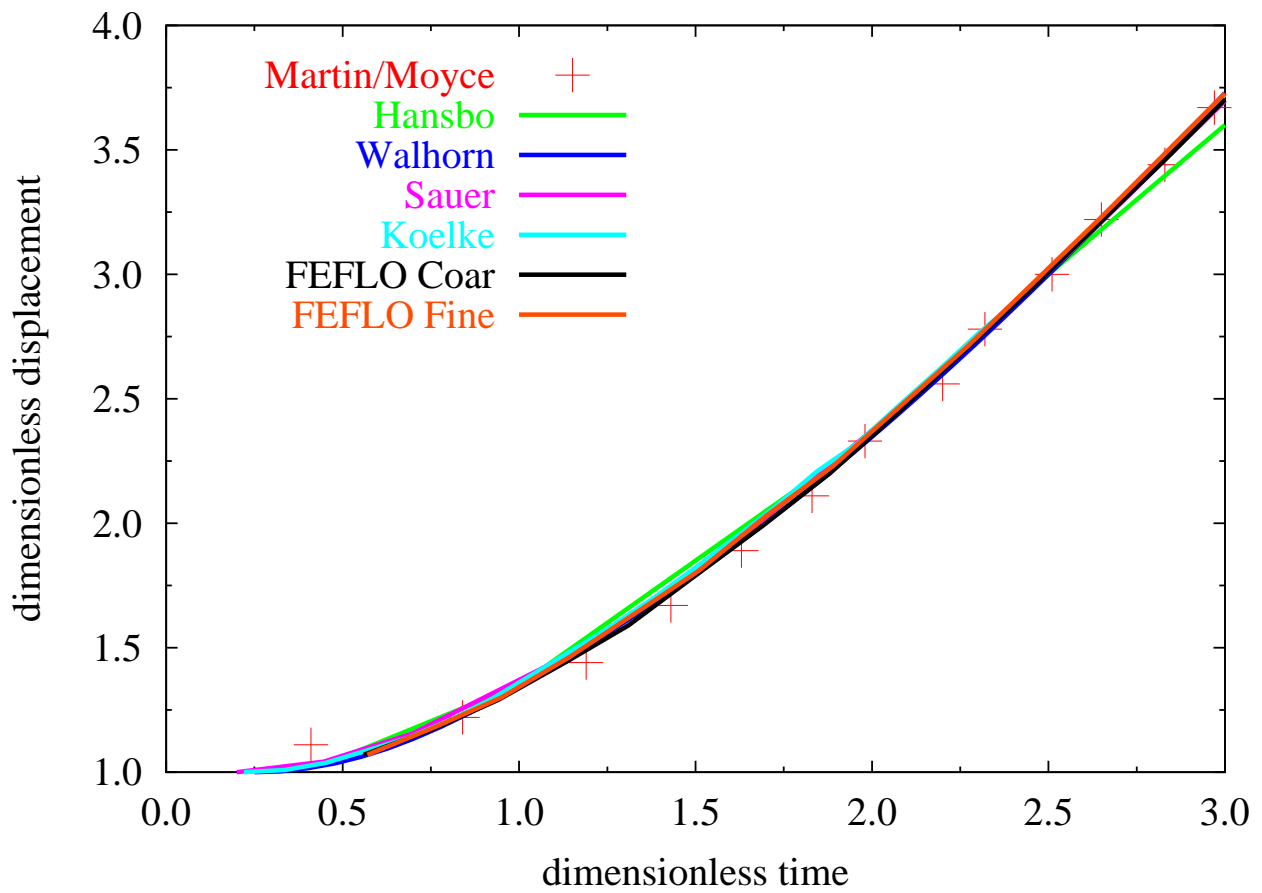
- Classic Testcase
- Some Experimental Measurements

BREAKING DAM (2)



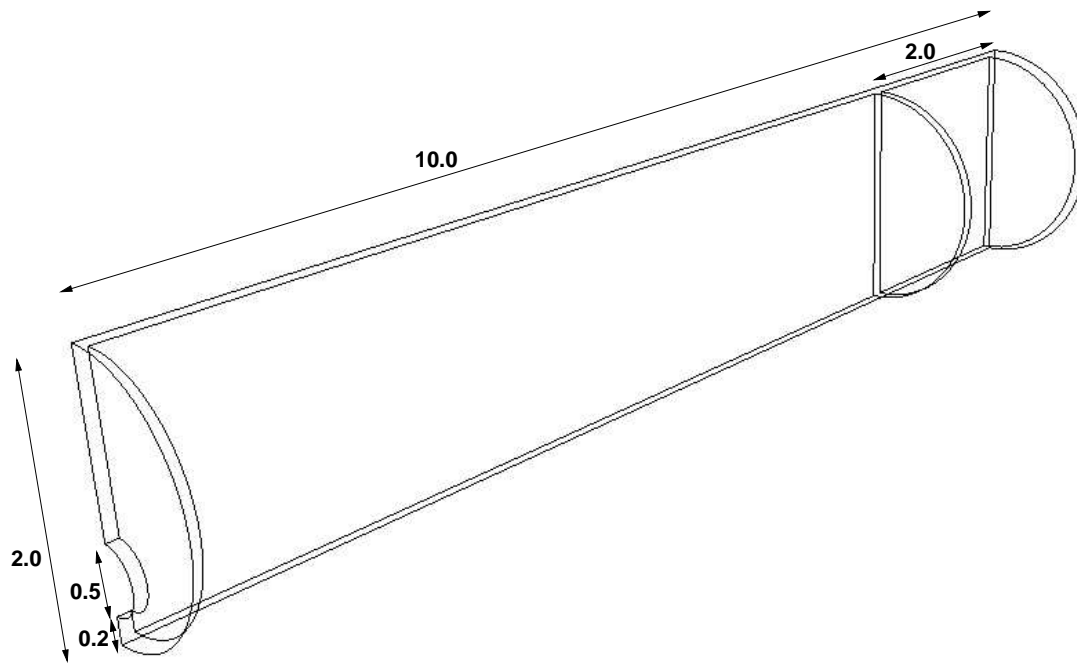
Breaking Dam: Flowfield at Different Times

BREAKING DAM (3)



Breaking Dam: Horizontal Displacement

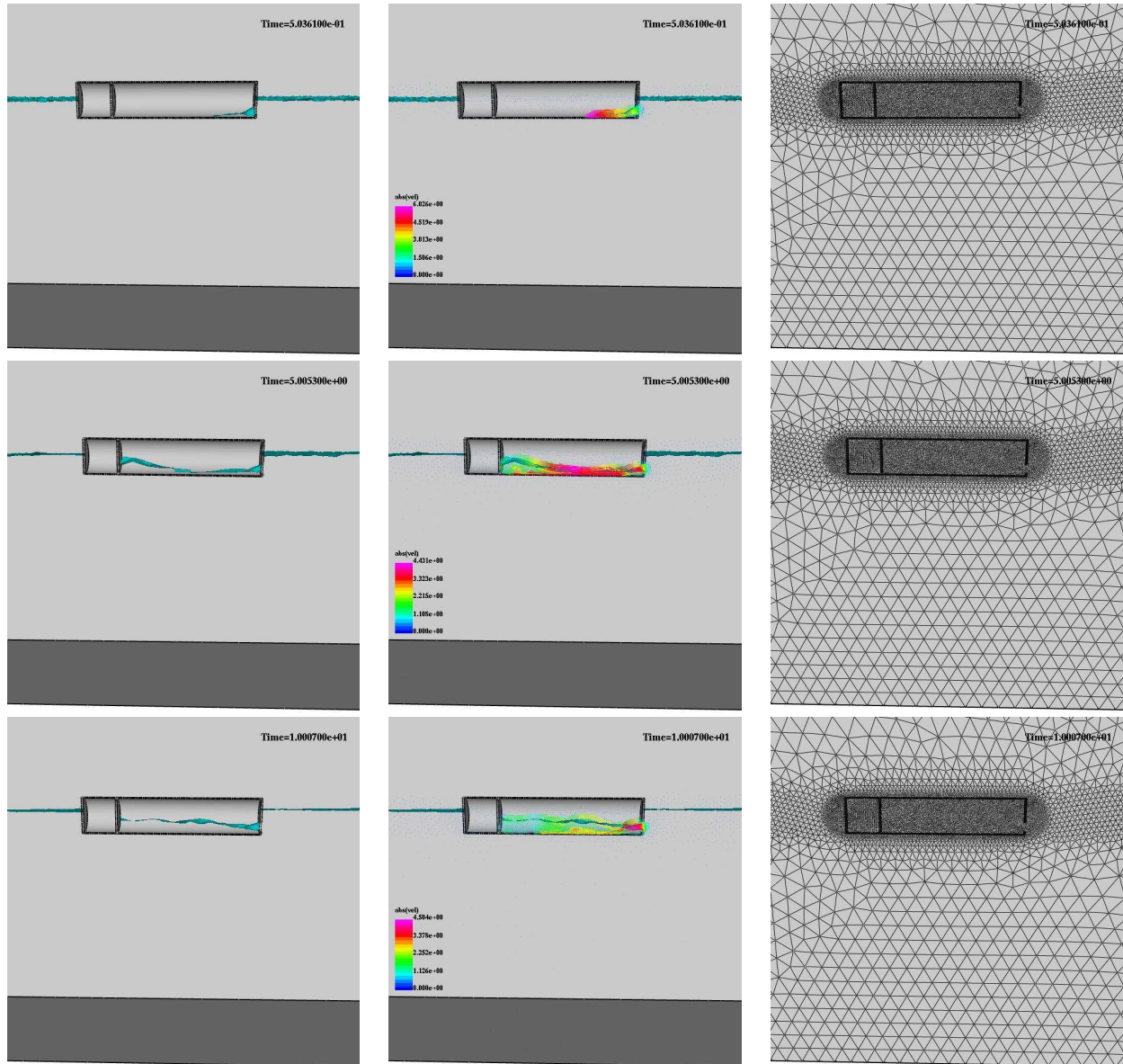
SINKING TANK (1)



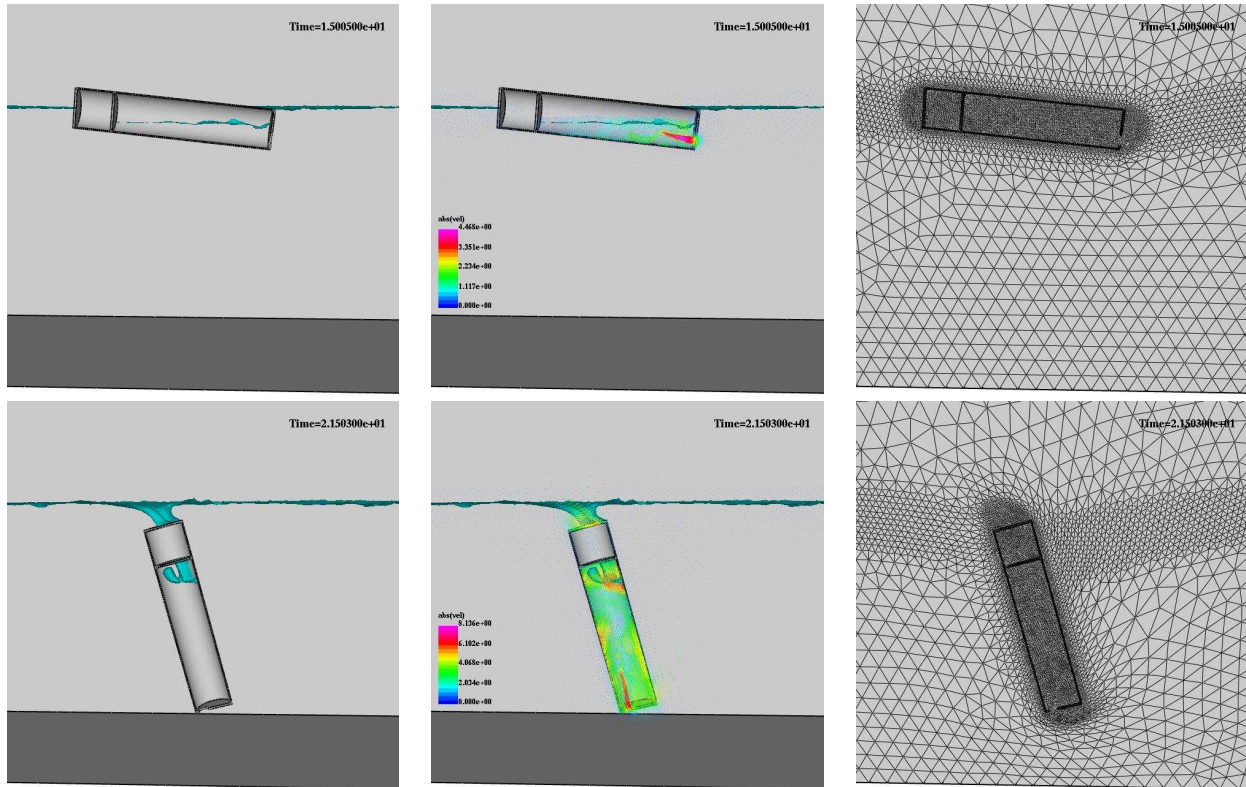
Sinking Tank: Problem Definition

- Moving Body
- ALE
- Automatic Remeshing

SINKING TANK (2)

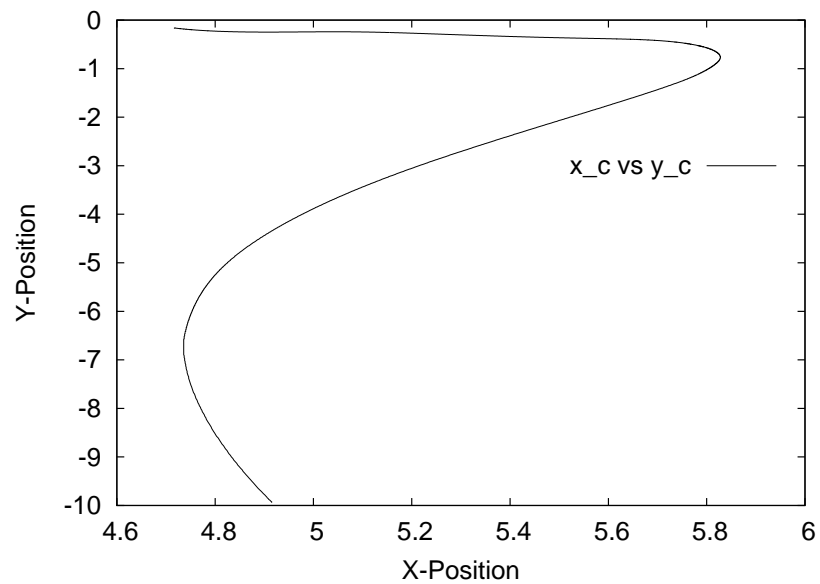
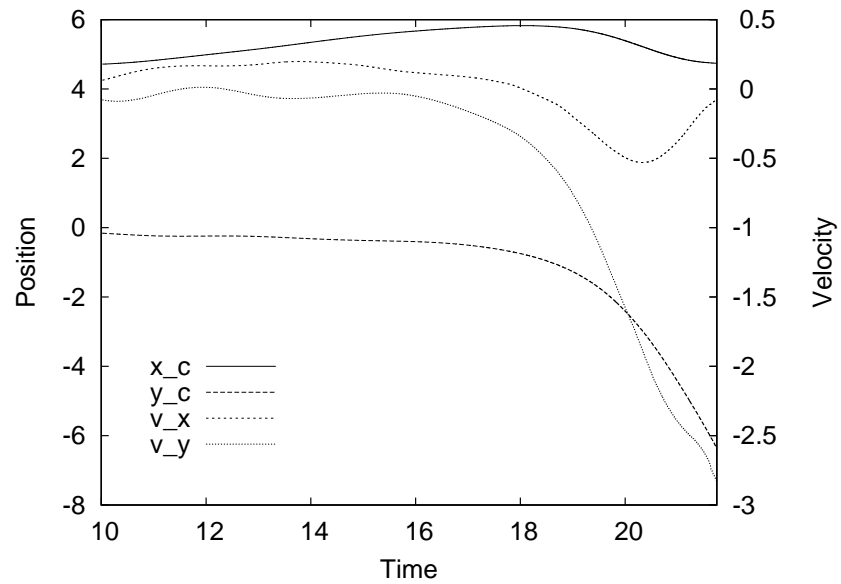


SINKING TANK (3)



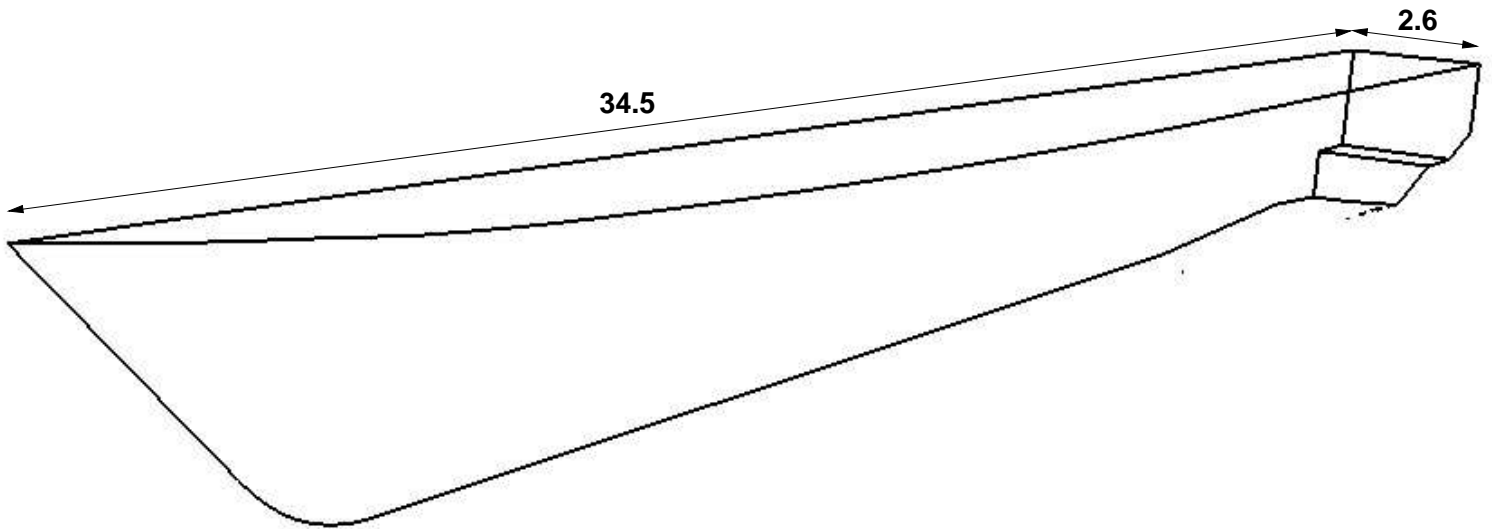
Sinking Tank: Flowfield at Different Times

SINKING TANK (4)

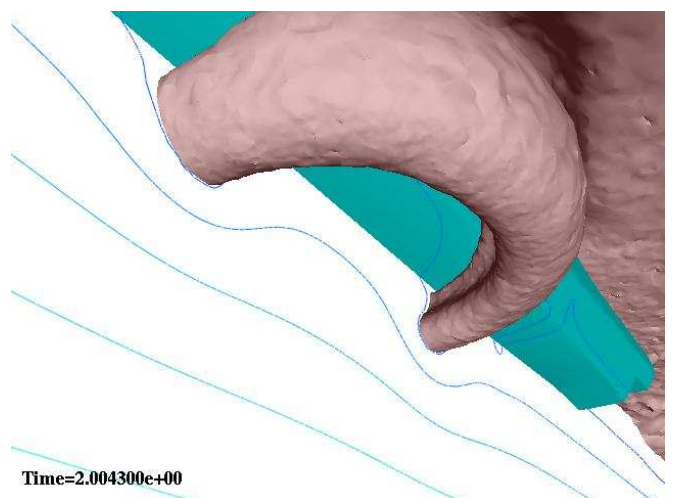
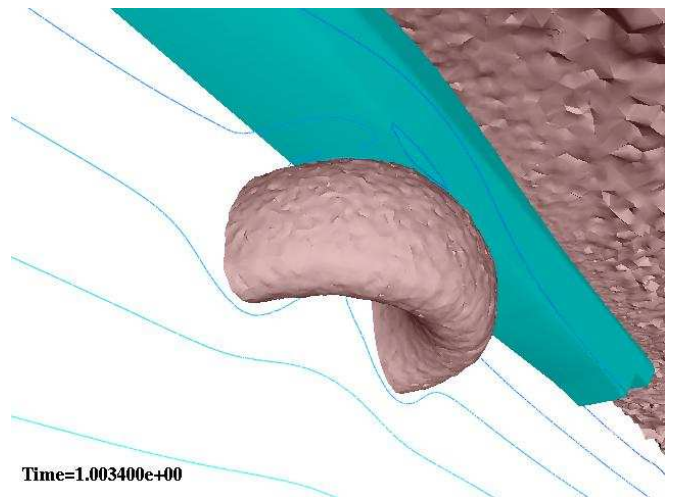
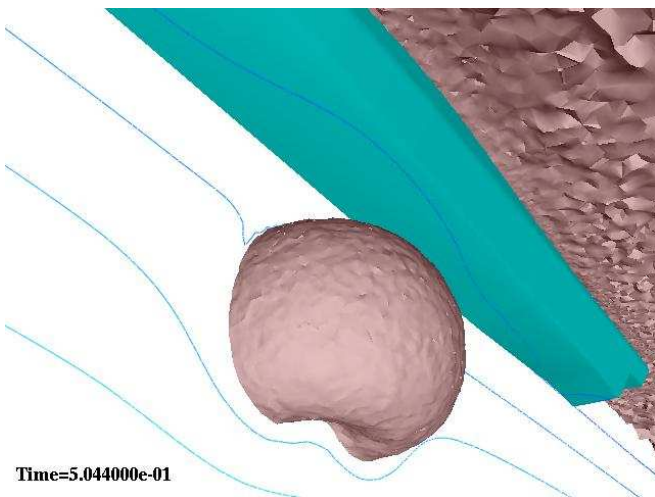
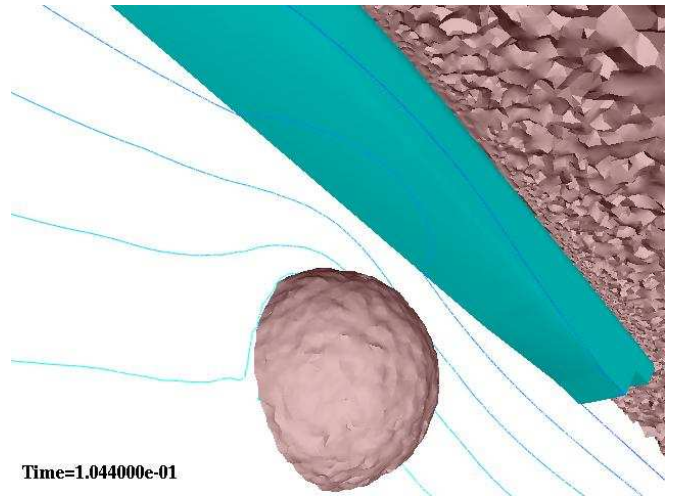
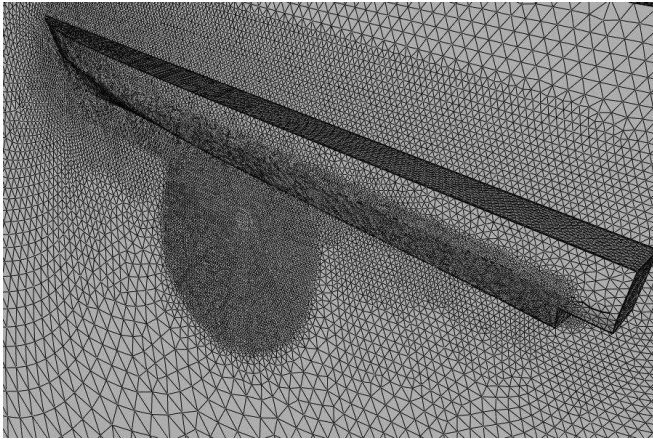


Sinking Tank: Trajectory of Center of Mass

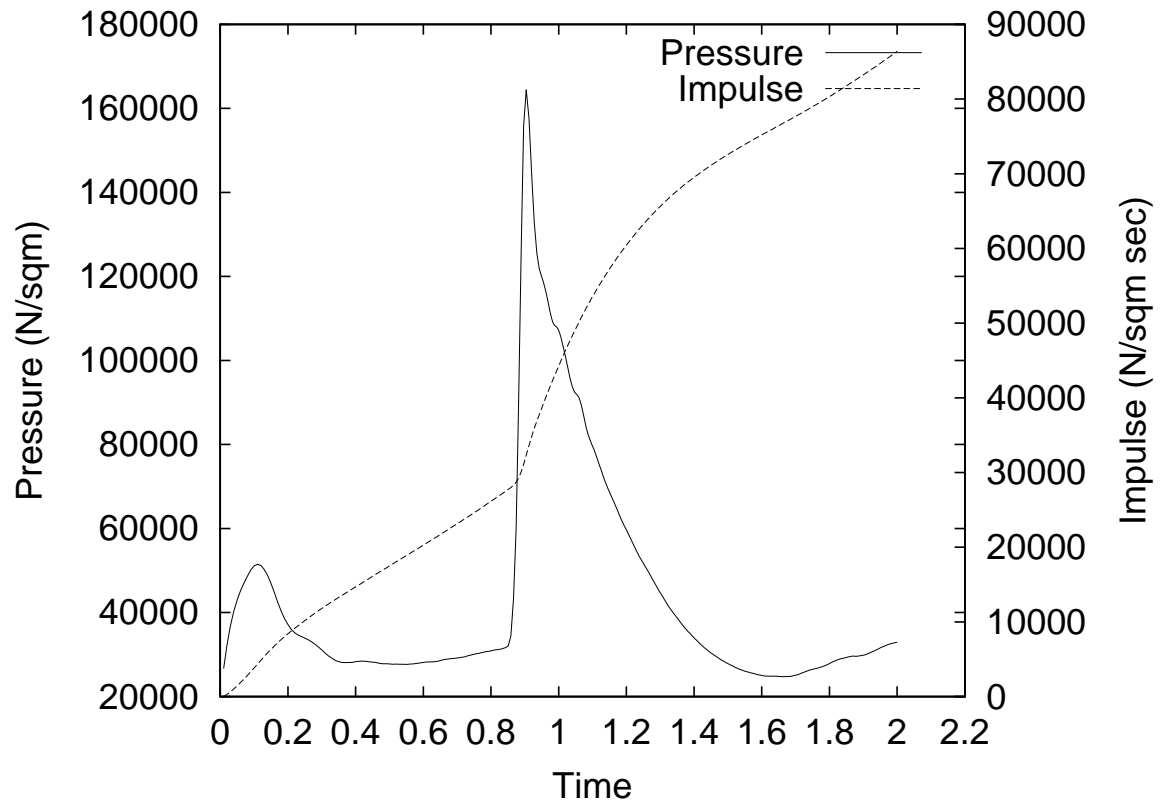
BUBBLE COLLAPSE (1)



Bubble Collapse: Problem Definition



BUBBLE COLLAPSE (3)



Pressure and Impulse Recorded at Midship on Hull