

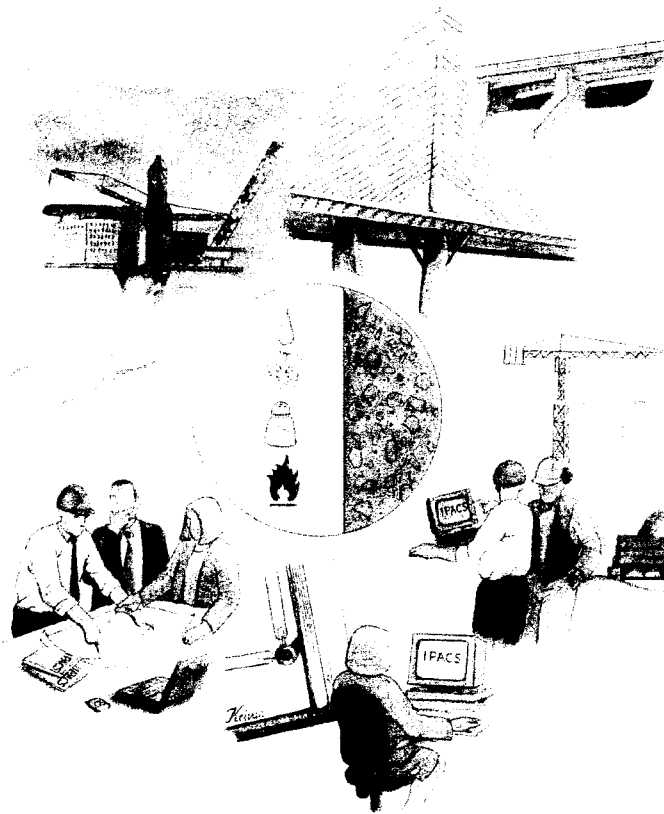


*Improved Production of Advanced
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Engineering Models for the Assessment of Restraint of Slabs by Soil and Piles During Early Age of Concrete



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