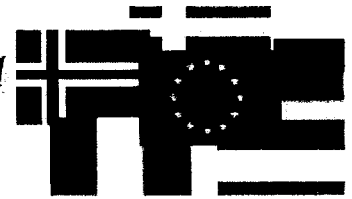


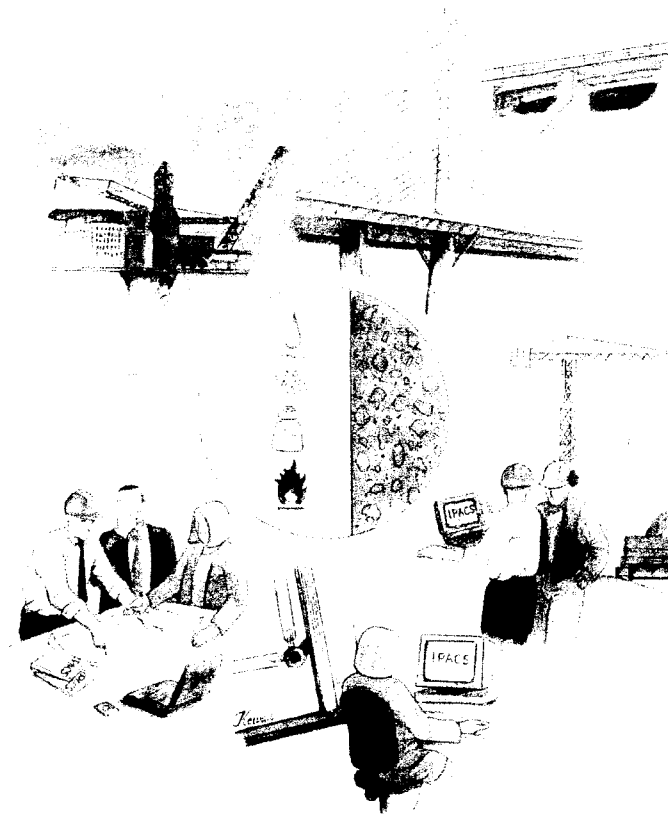


**Improved Production of Advanced  
Concrete Structures -IPACS**



REPORT BE96-3843/2001:35-4

# ***Computation of Stresses and Cracking Criteria for Early Age Concrete – Methods of iBMB –***



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