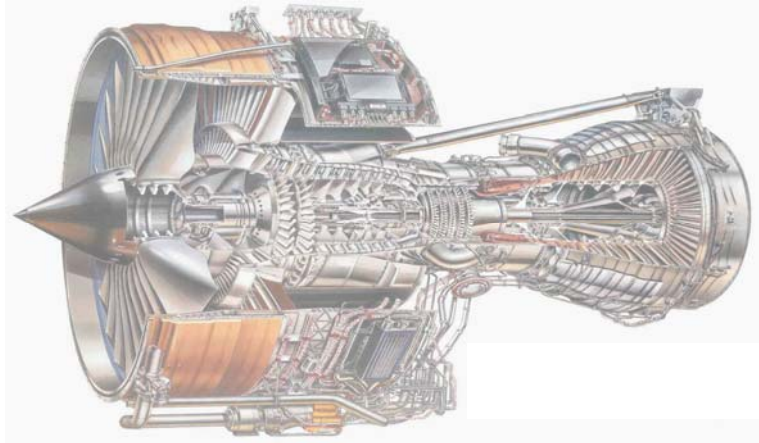


Paul Tucker, Simon Eastwood, Christian Klostermeier
Hao Xia, Prasun Ray, James Tyacke and William Dawes

Whittle Laboratory, University of Cambridge



Summary

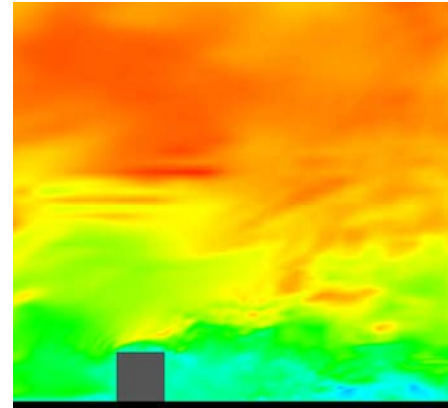
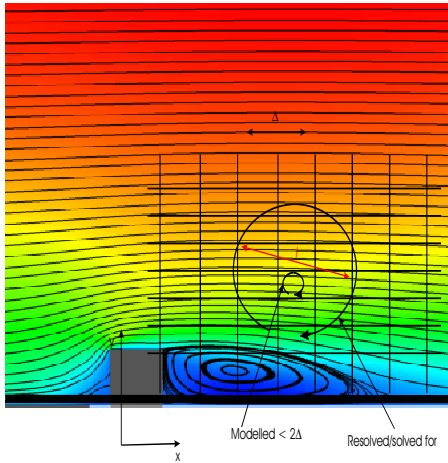
- LES computational cost discussed
- LES hierarchy is proposed → LES model last !!
- Practical hybrid LES approach is proposed
- Applied to predict canonical flows: HDT, free shear flow, wall shear flows (+TS), ribbed passage; convex surface impingement
- Consider turbine and compressor endwall flows; fan blade section; jets; cutback trailing edge; idealized high pressure compressor drum cavity
- Encouraging results. Challenges remain for complex BL physics
- Need for best practices, better validation data discussed



What is LES, MILES, NLES ...?

RANS = Resolve time average of flow, all modelling

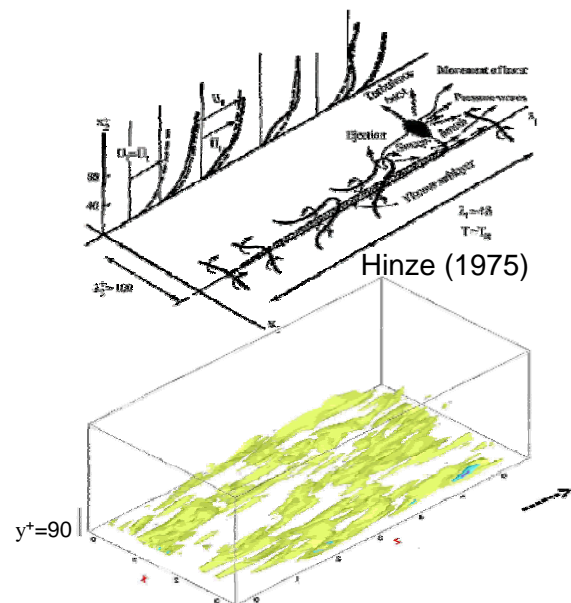
LES = Resolve all large eddies 10% modelling



- Practical LES (DeBonis)
- Rigorous LES

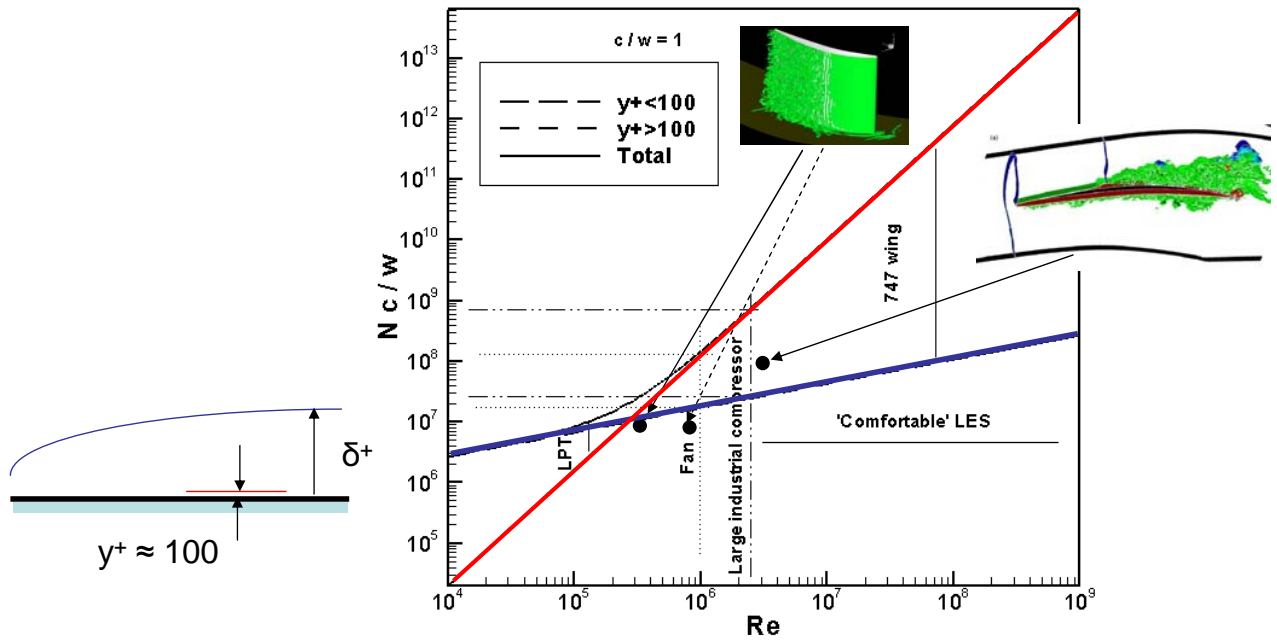
KEY LES PROBLEM

- Resolving streaks $\Delta z^+ \approx 100$
- Trent 1000 fan at cruise 10^7
- LES Cost $\propto Re^{2.5^*}$
- Hybrid LES-RANS Cost $\propto Re^{0.5}$



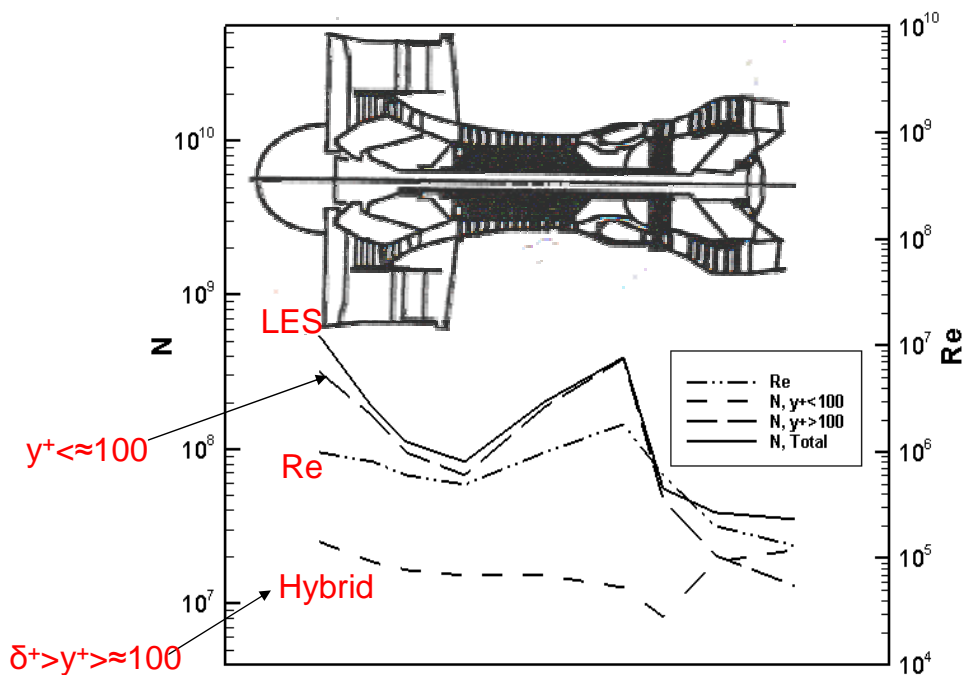
*Piomelli, AIAA-2008-396

LES Resolution Requirements



Adapted from Leschziner (2009), Piomelli and Balaras (2002)

Grid Requirements



NUMERICS/SGS SENSITIVITY

Range of Solvers

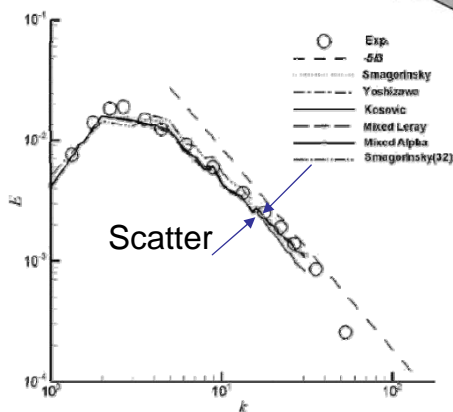
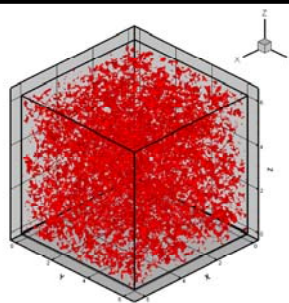
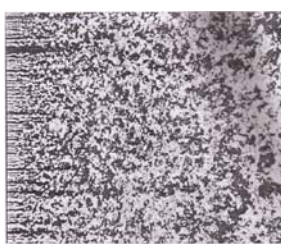
Code	Description	Order of Φ_{ctr}	Smoothing
HYDRA	Cell Vertex	2	4th order
BOFFS	Curvilinear	2-6	3-7th order
FluxP	Cell Centered	2	4th order
TBLOCK	Cell Vertex	2	4th order
CHYDRA	Cell Vertex	2	f(wiggles)
Vu40	Staggered Grid	2-8	Smag. Model

Range of LES Models

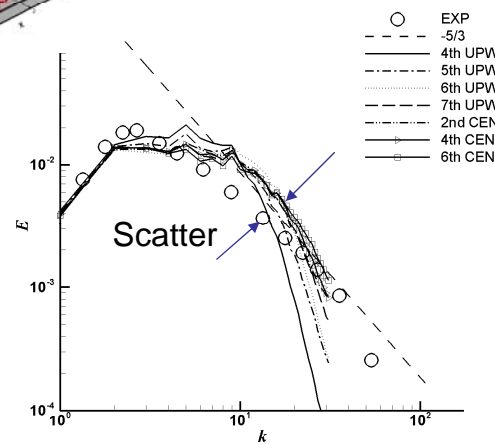
Model	Components
Smagorinsky	L
Yoshizawa	L
Clark	L+NL
Kosovic	L+NL
LANS- α	L+NL
Leray	L+NL
VMS	Uses Smag. Model

Liu, Y., Tucker, P. and Kerr, R. Linear and nonlinear model large-eddy simulations of a plane jet. *Computers and Fluids*, 37(4): 439-449, 2008

Homogenous decaying turbulence



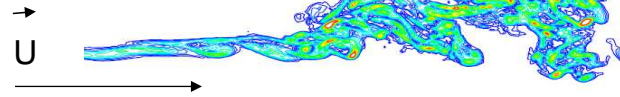
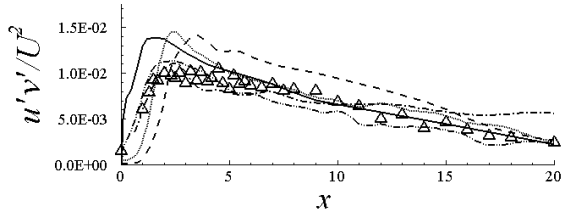
LES model



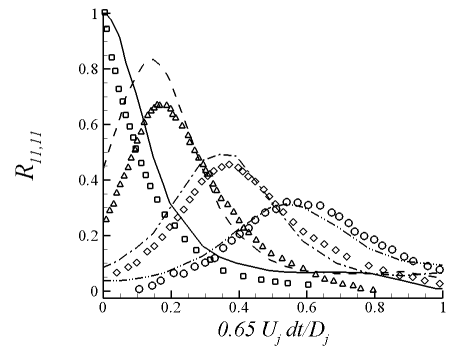
Numerical parameters

Shear Layers – significant numerical influence

- Average predicted shear stress error for five LES models, five numerical schemes and 10% Ti delt inflow



	Std. Dev.	Ave. error
LES model	4 %	12 %
Numerical scheme	19 %	14%
Inflow (Ti = 10%)	-	4 %

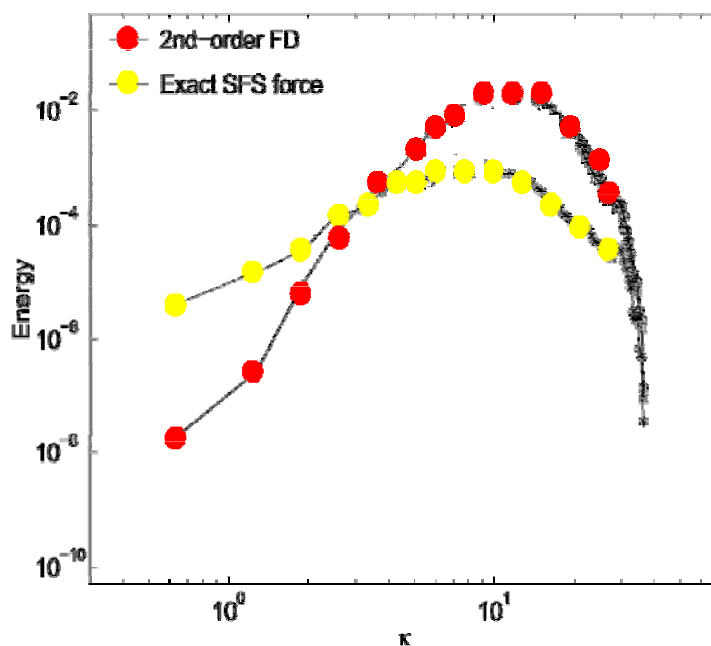


For NLES $N/Re^{0.4}$ - 3.5 time higher i.e. better resolved

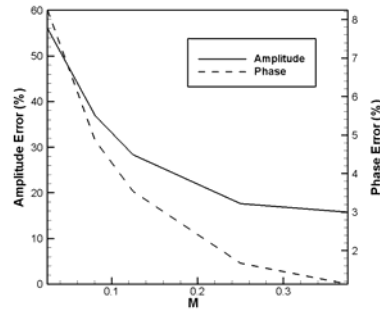
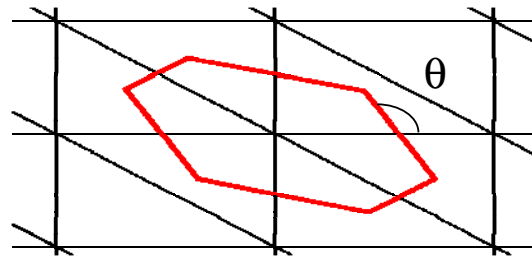
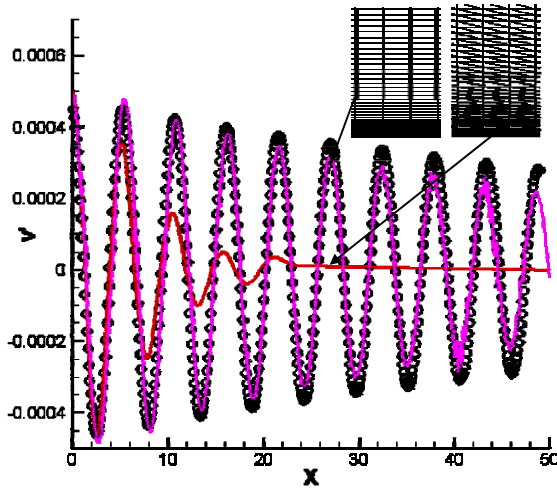


Shear Flow - Significant Numerical Influence

Chow and Moin JCP (2003) – numerical error



TS Wave in Shear Flow - Grid-Solver Compatibility/Sensitivity

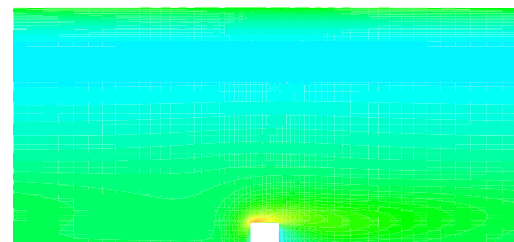
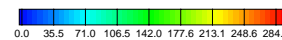
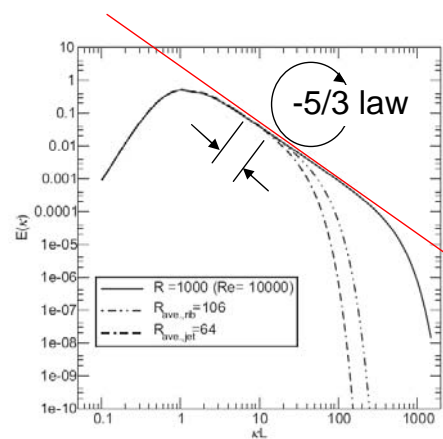


OMIT LES MODEL TO LESSEN DISSIPATION?

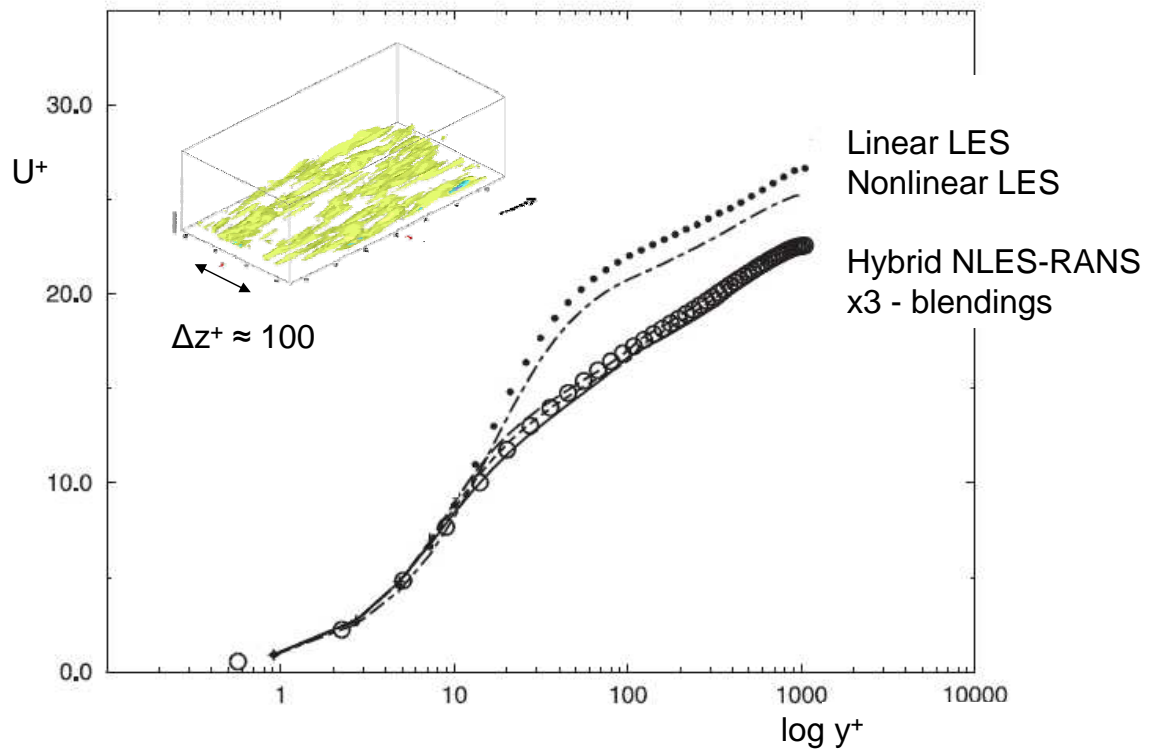


LES Model Validity? Omit?

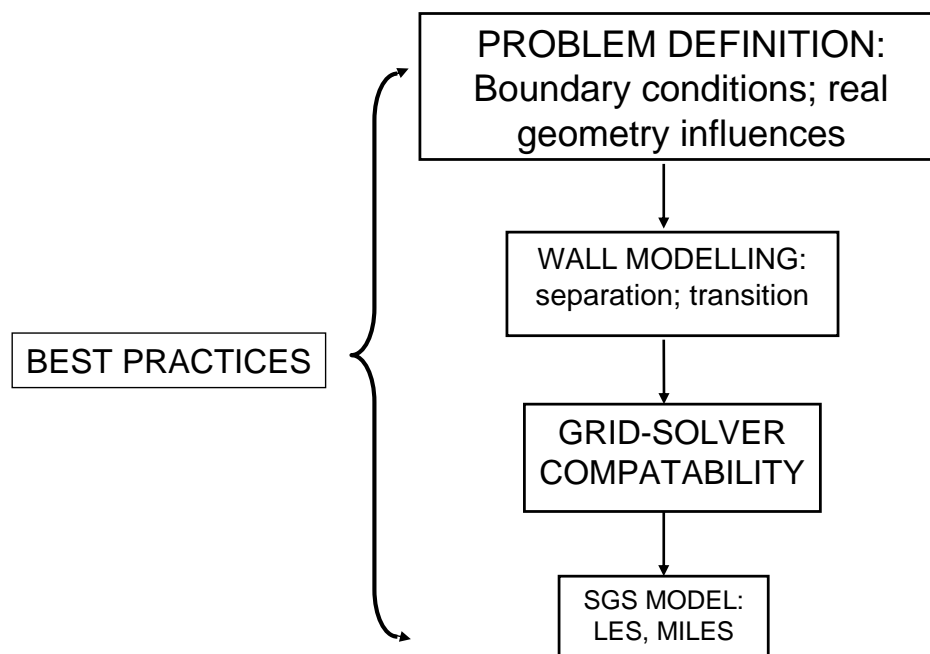
- Smagorinsky model erroneously drains energy from all scales (AIAA ban)
- It provides no backscatter
- Eddy viscosity alters the effective Reynolds number and so alters the fine scales (non-linear LES models OK?)
- Existence of Kolmogorov -5/3 region in turbomachinery? If not new LES model needed



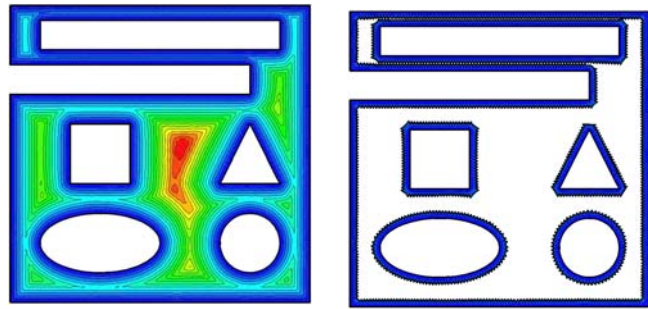
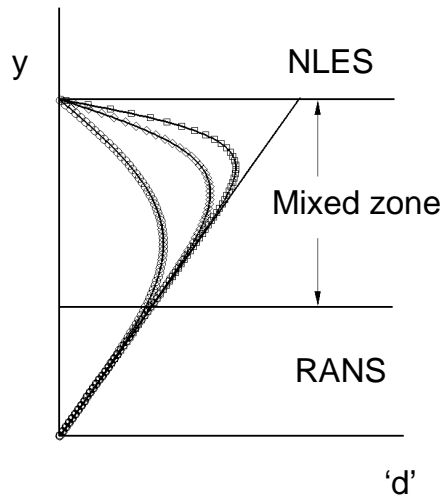
'Law of the wall' for under-resolved LES grids



Industrial Turbomachinery LES Hierarchy

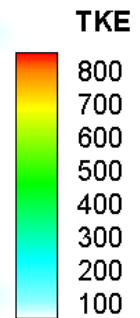
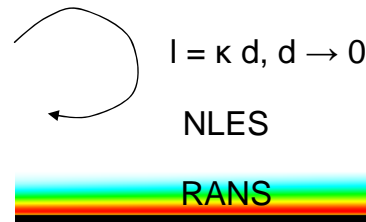


ENGINEERING MODELLING APPROACH – RANS-NLES Blending

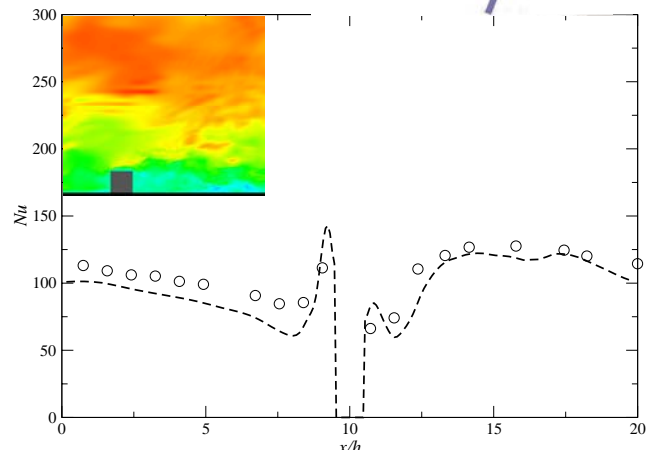
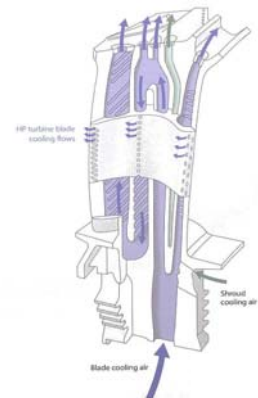
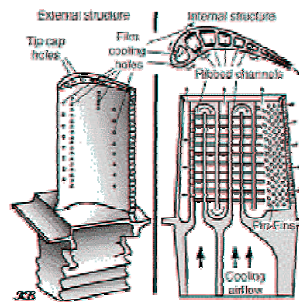
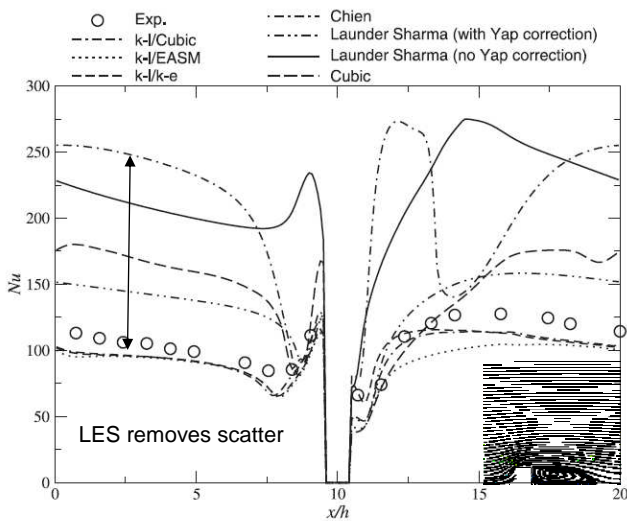


$$|\nabla\phi| = 1 + f(\phi)\nabla^2\phi + g(\phi)$$

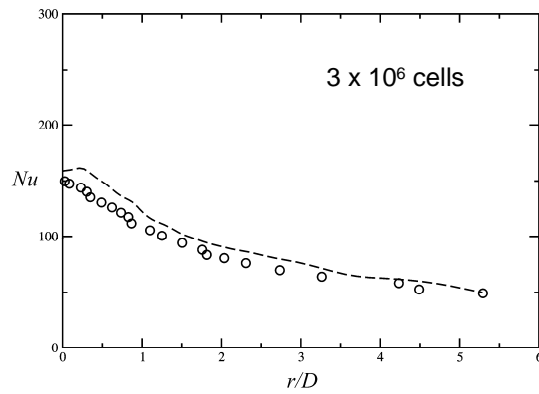
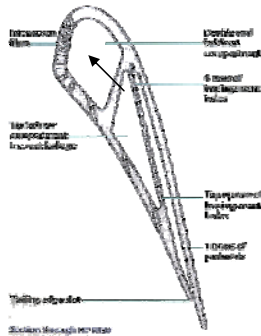
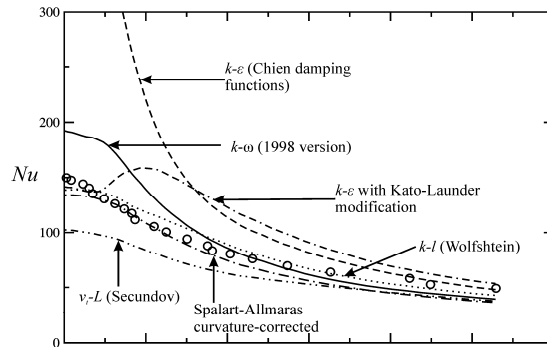
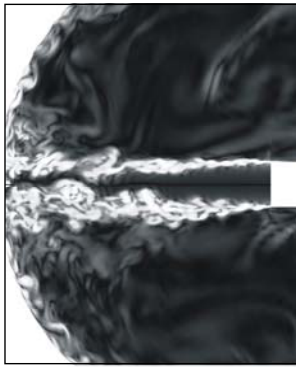
$$f(\phi) = \varepsilon_0\phi, \quad g(\phi) = \varepsilon_1(\phi/L)^n$$



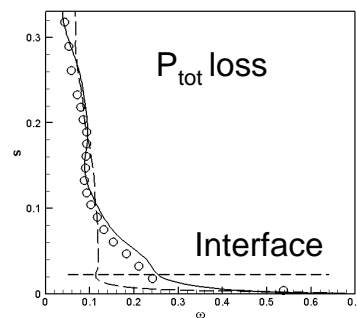
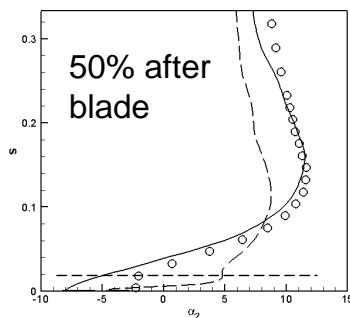
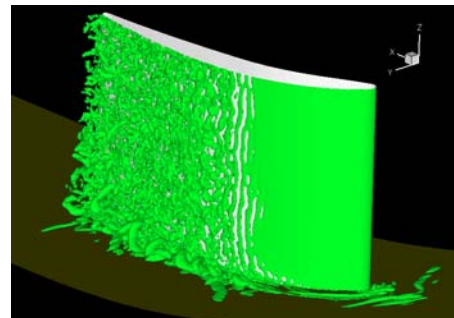
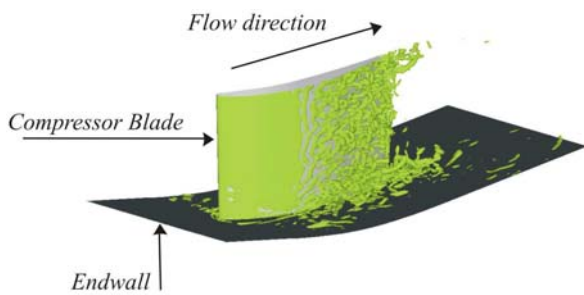
Ribbed channel (Re = 14,000)



Impinging Jet Flow – $Re = 23000$

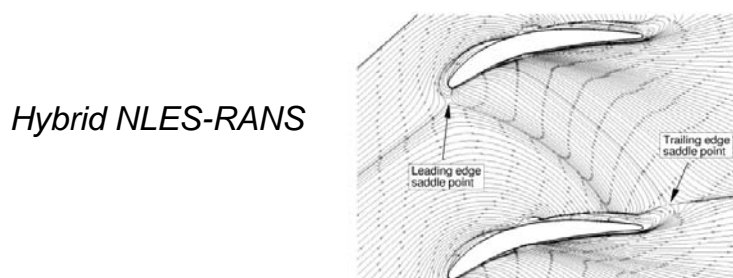
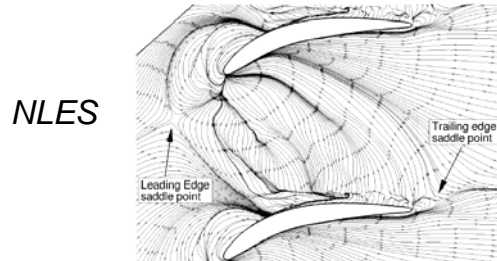
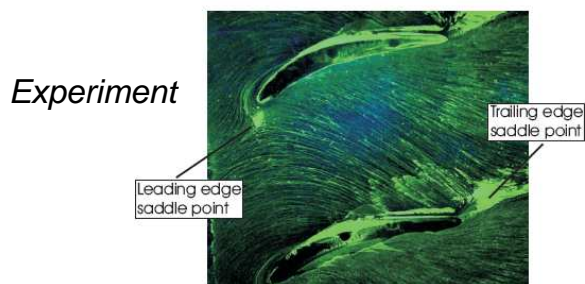


Compressor Blade – End Wall

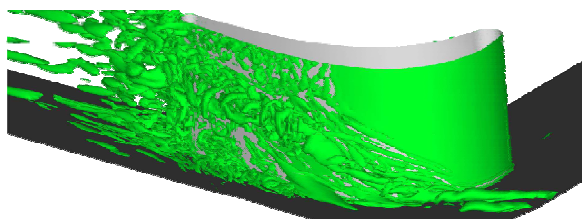


$Re \approx 0.25$ million, $N = 5$ million

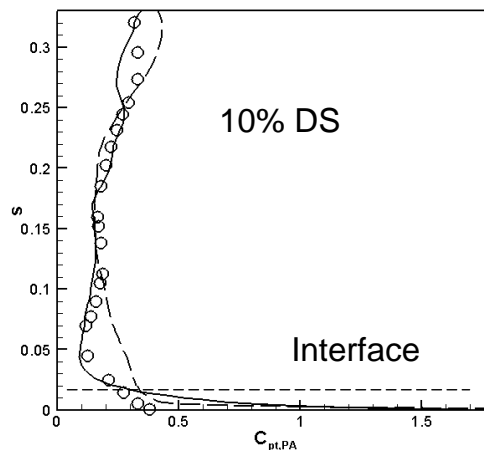
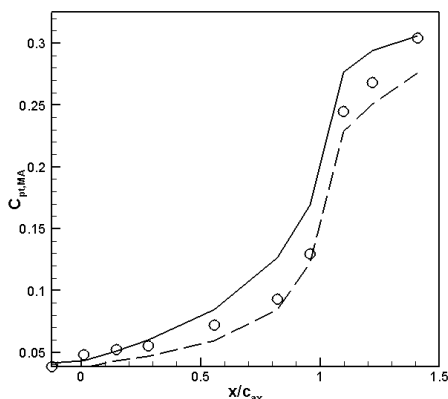
Streamlines at Endwall - Compressor



Averaged Total Pressure Loss Coefficient

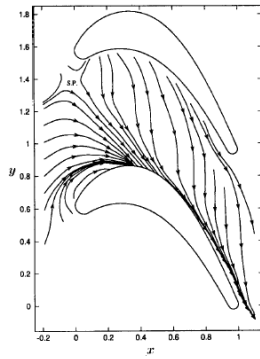


$Re \approx 0.6$ million, $N > 5$ million

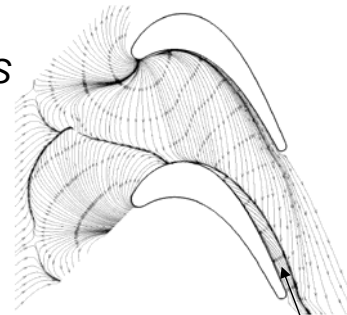


Streamlines at Endwall - Turbine

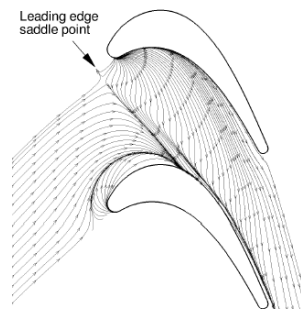
Experiment



NLES

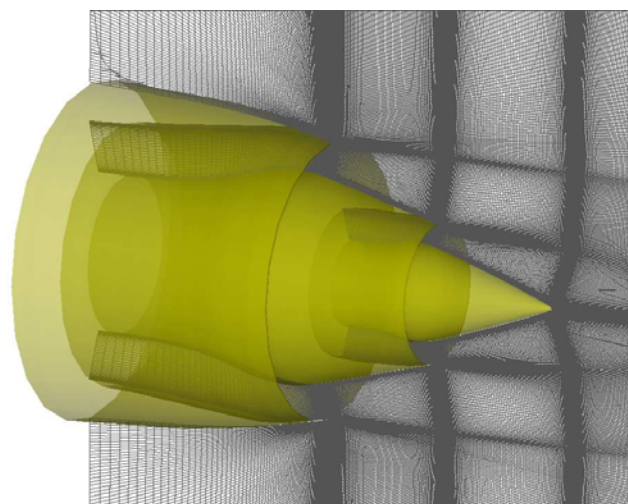
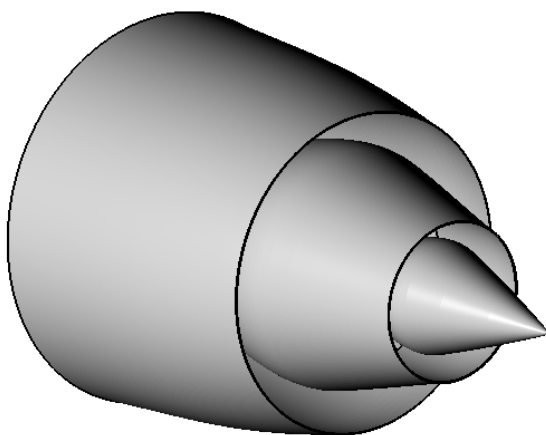


Hybrid NLES-RANS



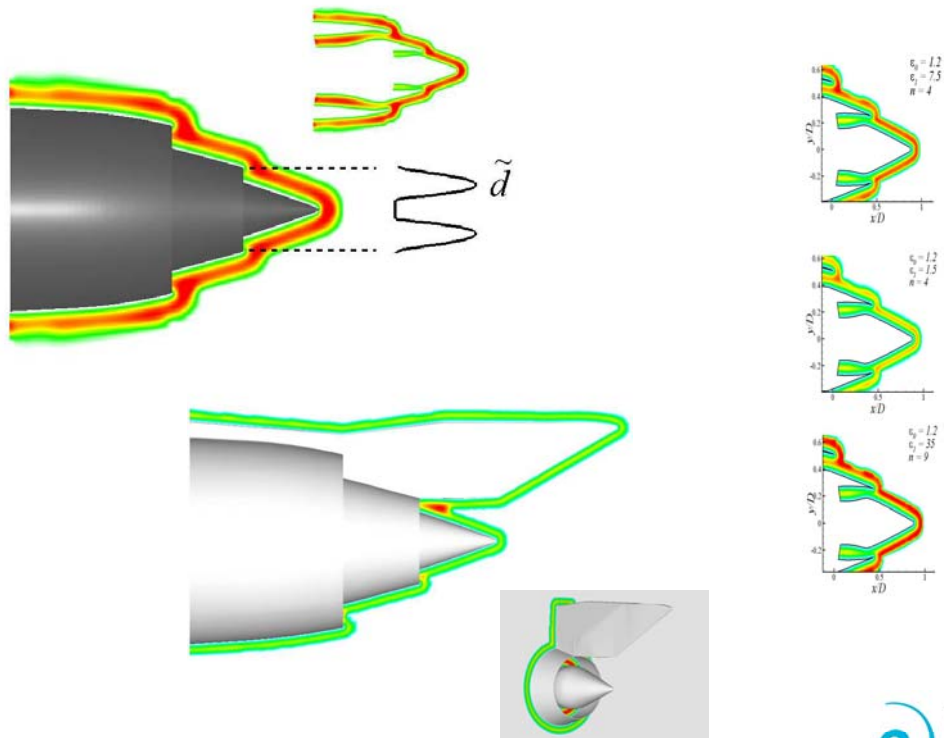
Excessive separation

Coaxial Nozzle

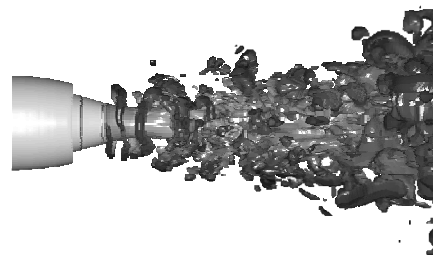
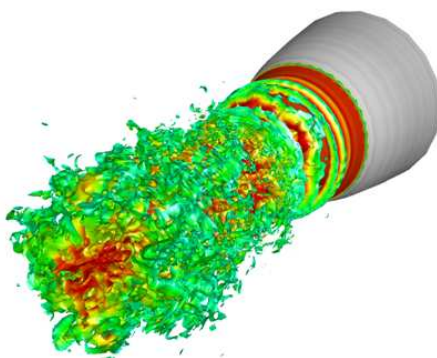
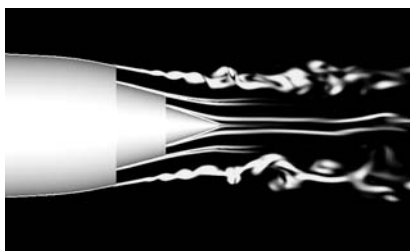


$Re = 300,000$, $5 < N < 50$ (million)

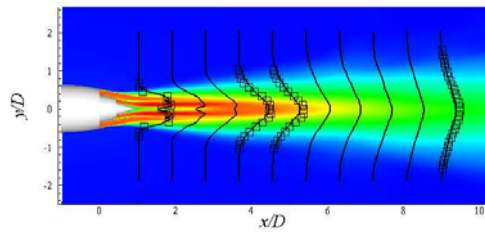
HJ Equation Distance Function



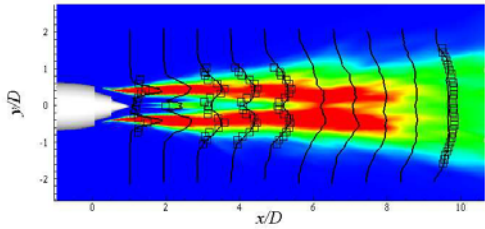
Vorticity Contours



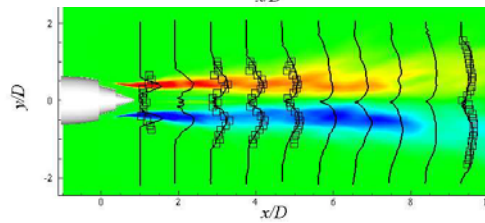
Statistics



Time averaged streamwise velocity.

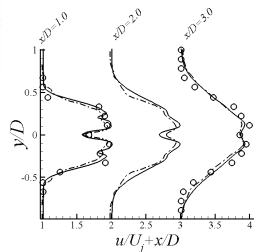
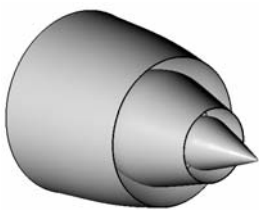


Normal stress, $u'u'$

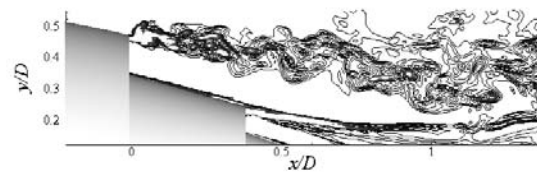


Shear stress, $u'v'$

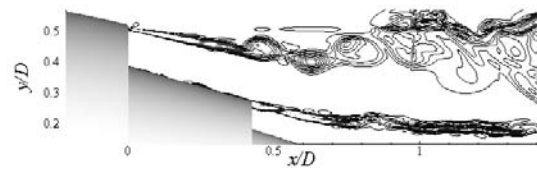
Grid Sensitivity



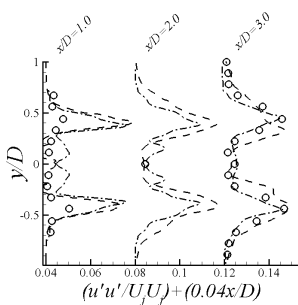
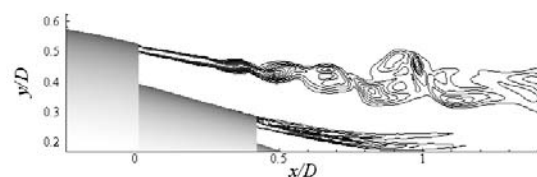
50M



12M

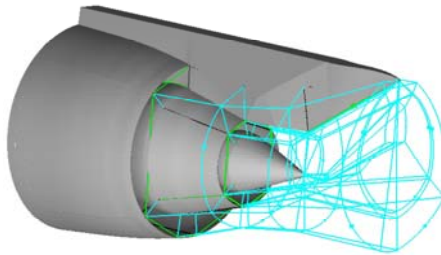


6M



SENSITIVITY TO REAL INFLOW/ GEOMETRY

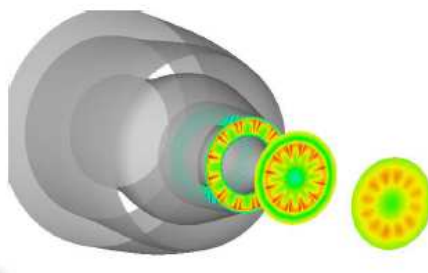
Geometry and
Blocking Structure



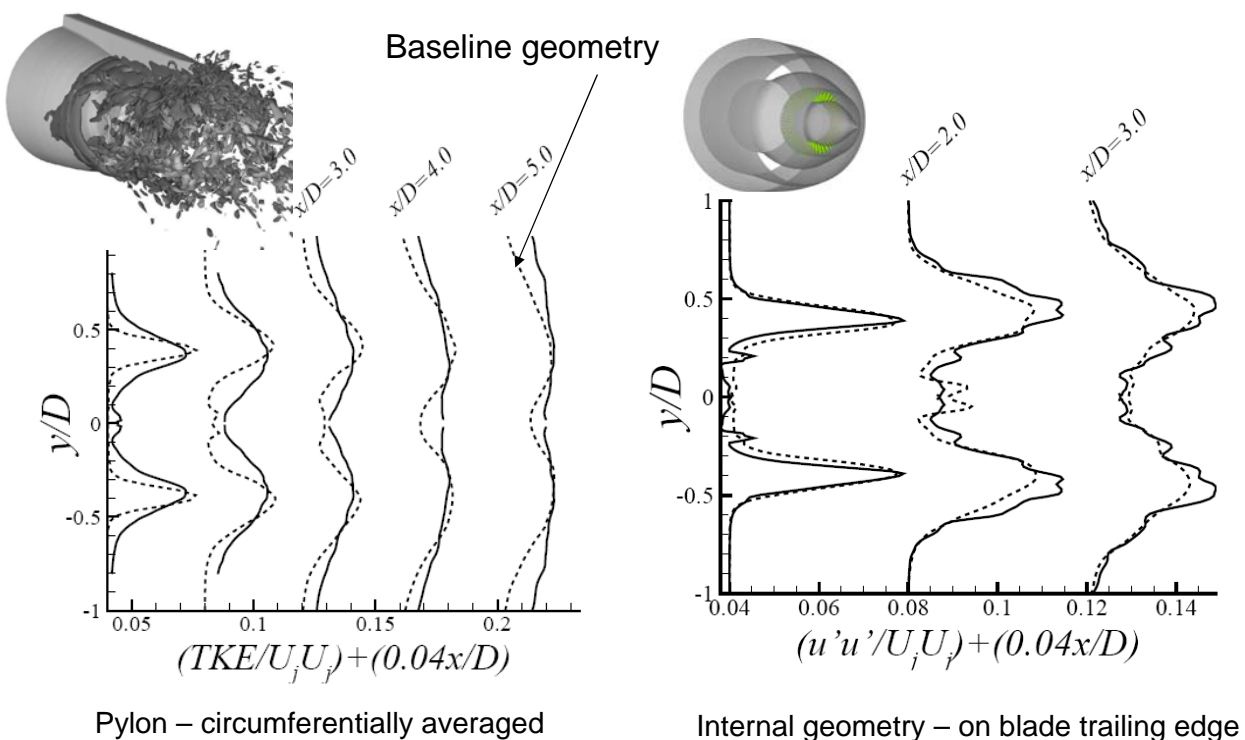
Vorticity Contours



Axial
velocity



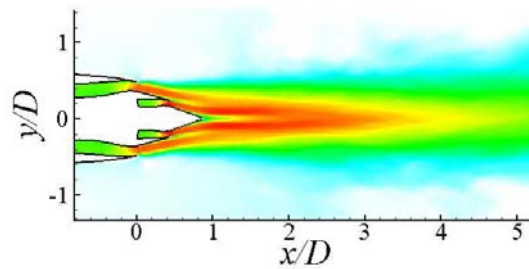
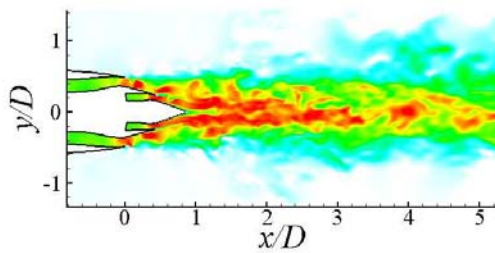
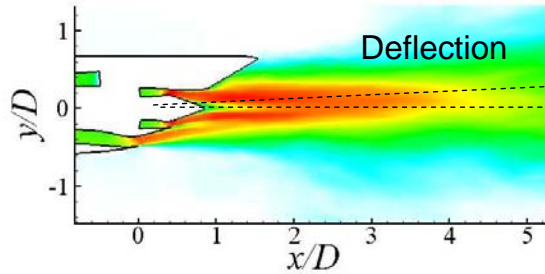
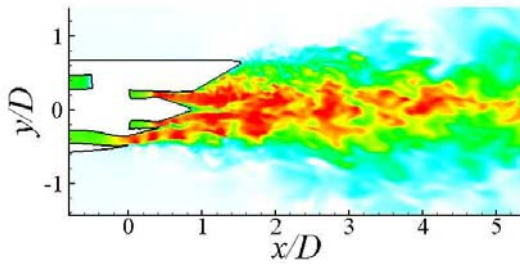
Turbulence profiles for pylon and nozzle with internal geometry



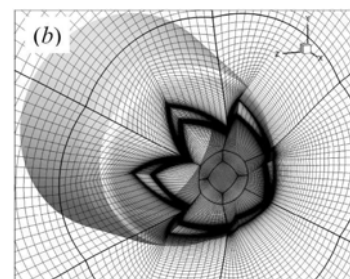
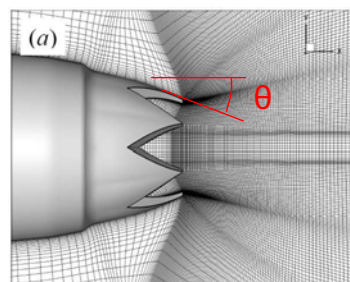
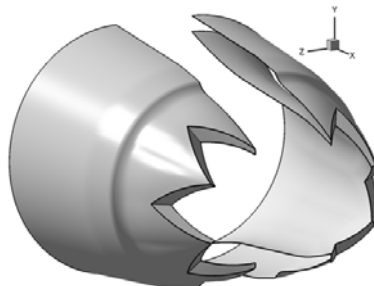
Pylon Geometry

Instantaneous Streamwise Velocity

Time Averaged Streamwise Velocity

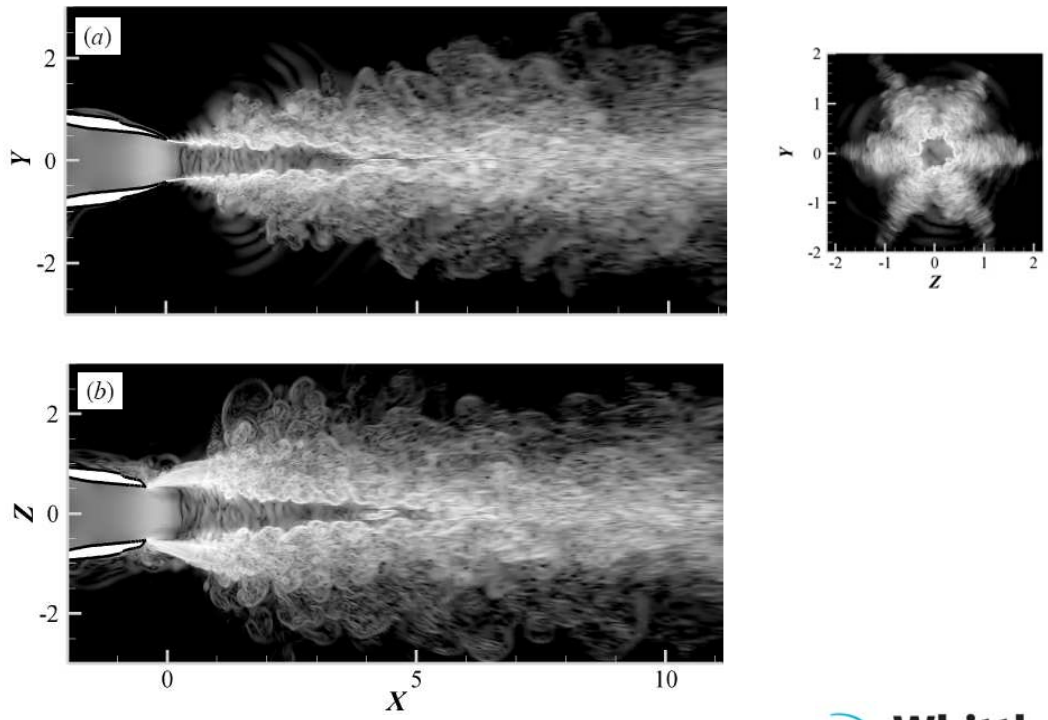


Chevron Nozzle

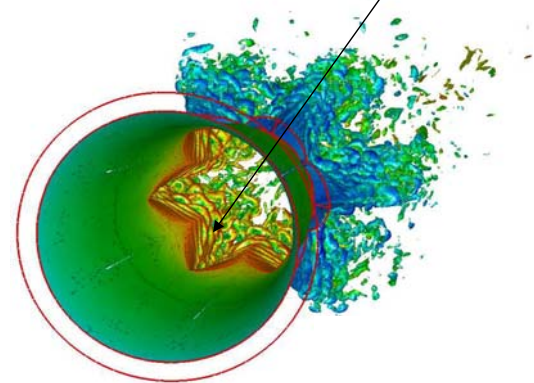
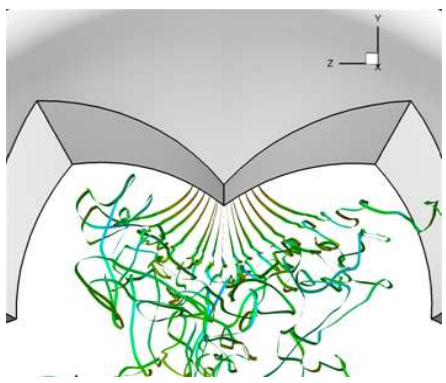
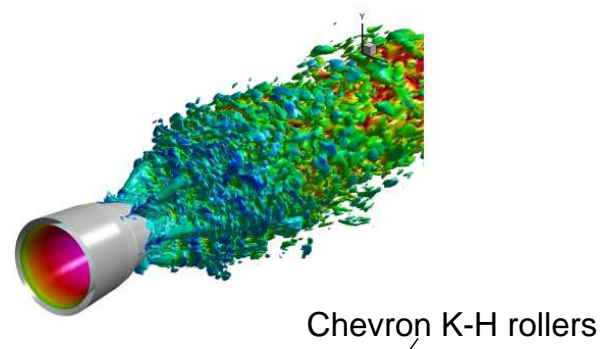
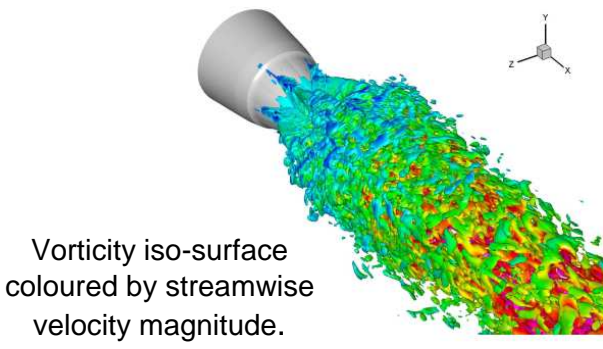


$$12 \times 10^6 < N < 60 \times 10^6, \text{Re} = 1 \times 10^6$$

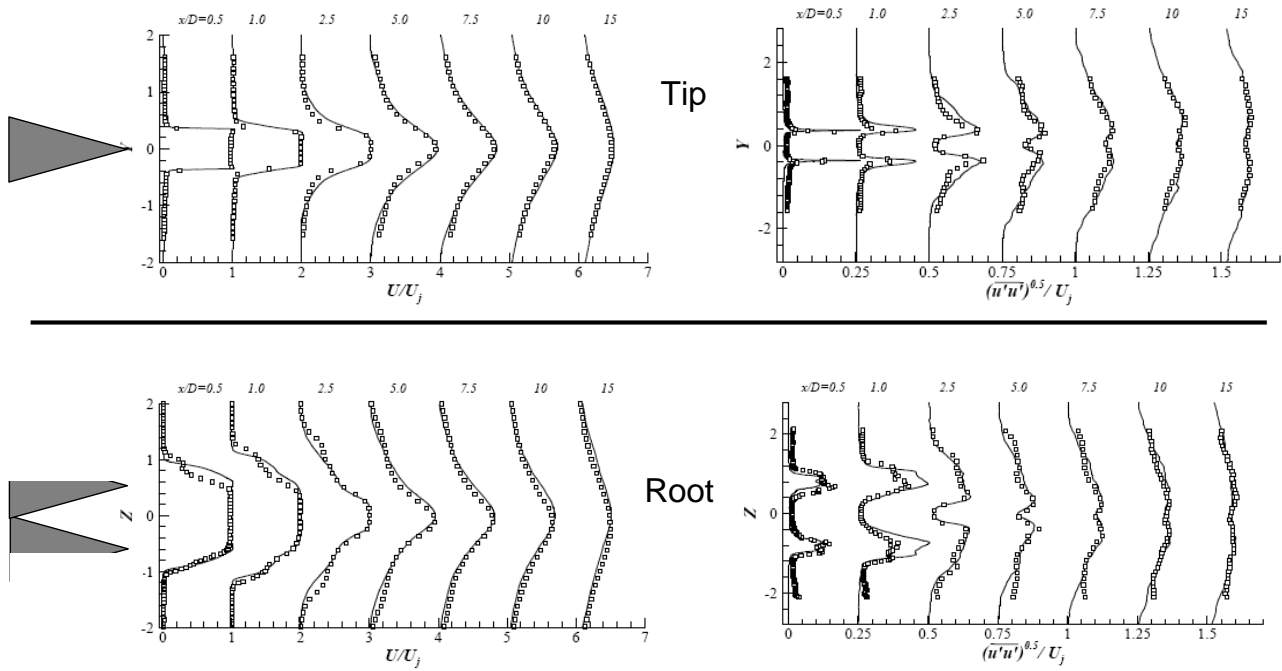
'Numerical Schlieren'



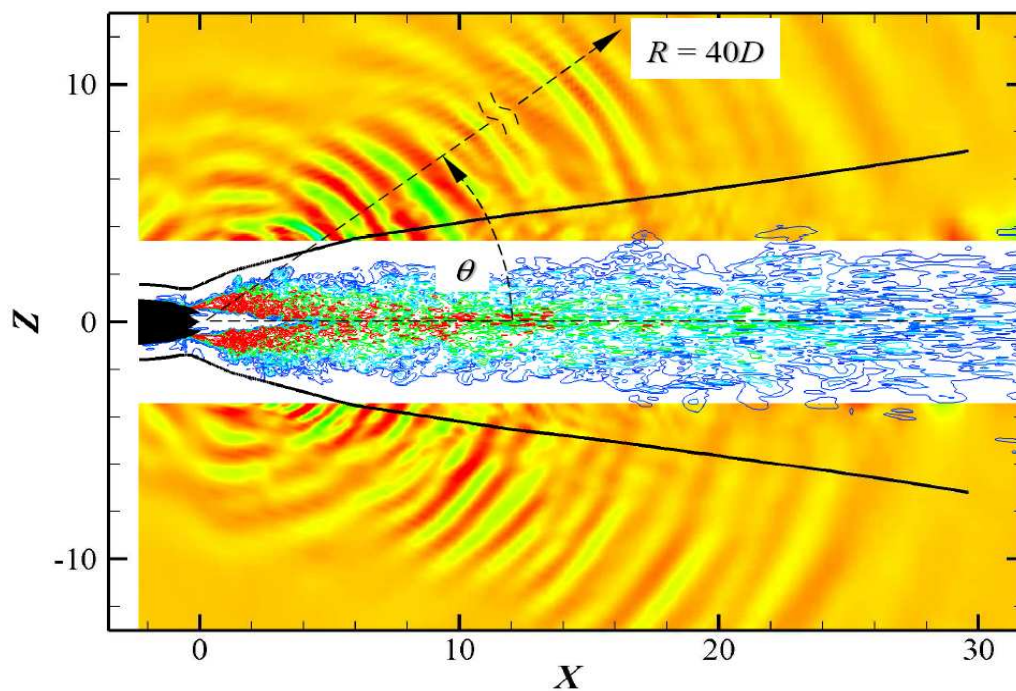
Flow Visualisation



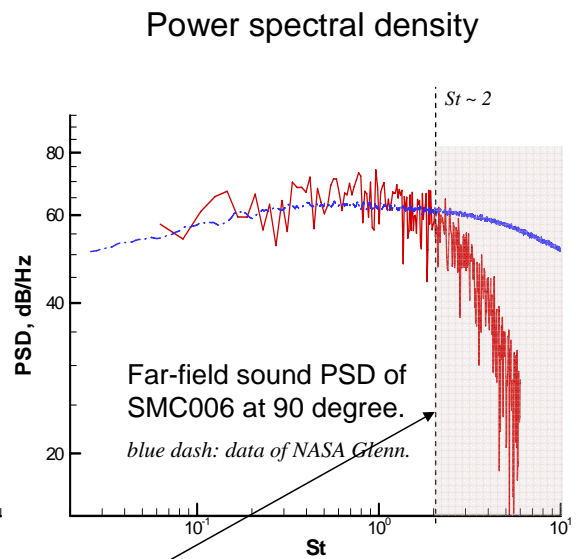
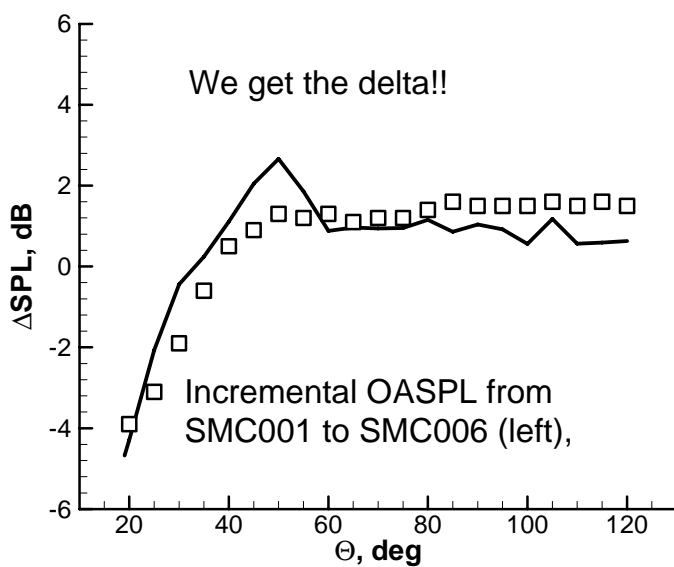
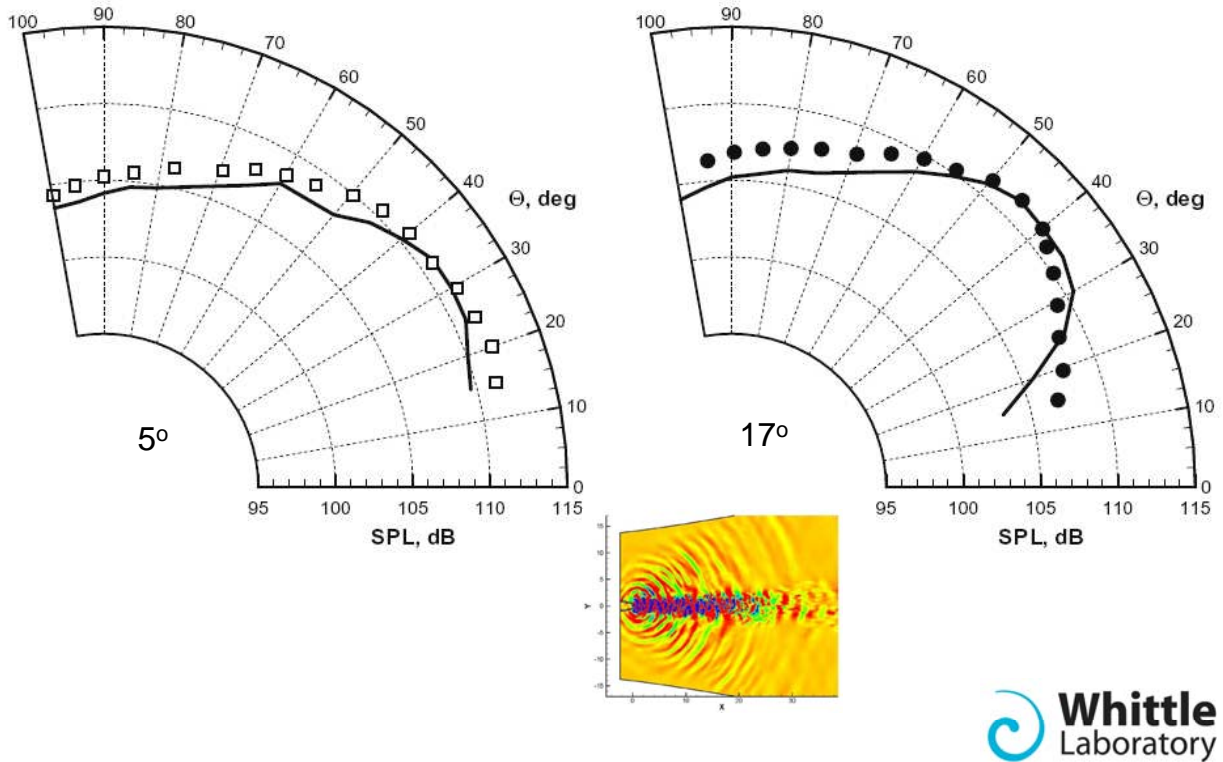
Statistics



RANS-LES + FWH



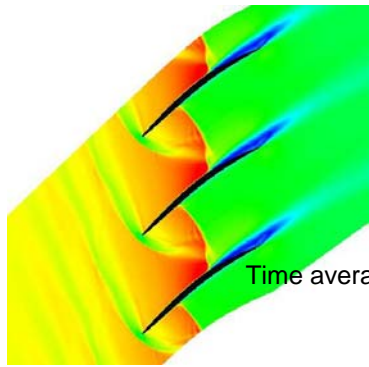
Chevron Far-field Sound (SPL)



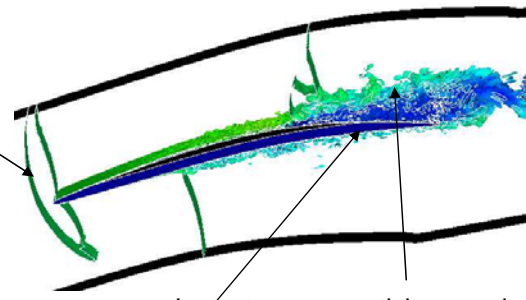
$$St_{max} < a_{\infty} / 4\Delta$$

Assume 4 nodes can resolve a wave accurately

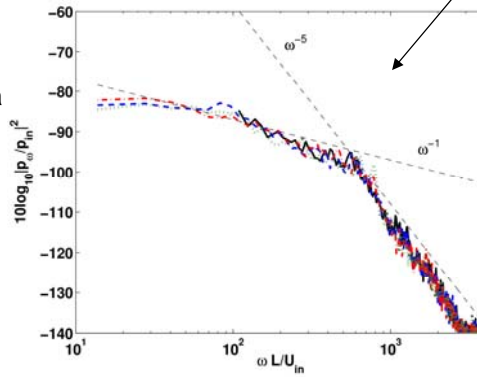
Fan Blade Section ($Re = 3 \times 10^6$)



M=1 isosurface



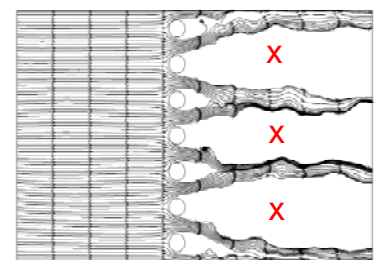
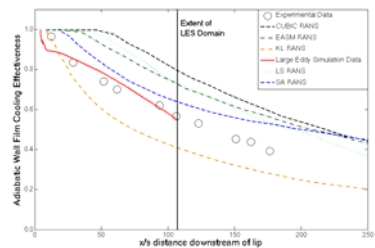
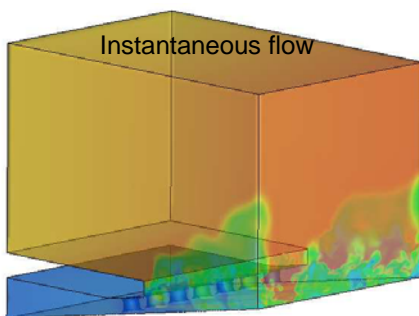
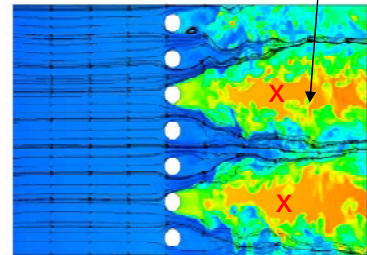
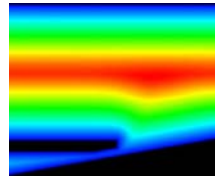
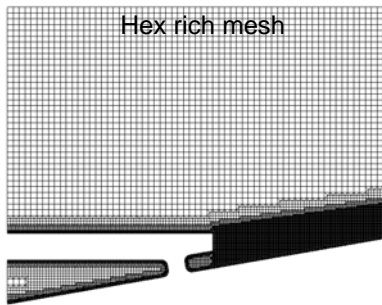
Blade surface pressure spectra



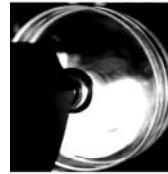
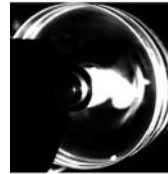
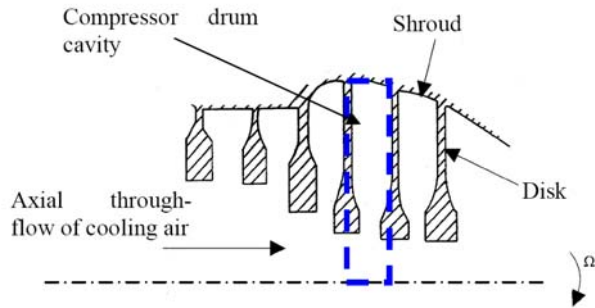
N = 8 million

Cut back trailing edge

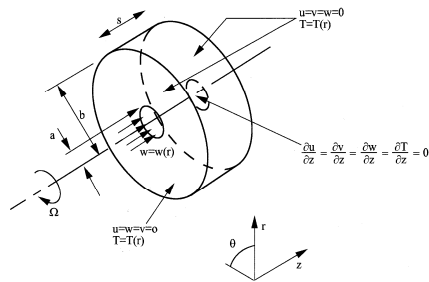
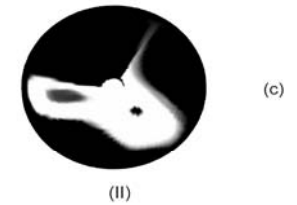
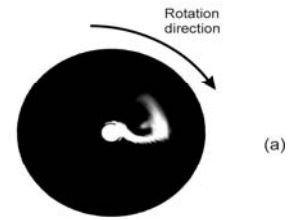
'Martini & Schultz' (2004) type case, Kacker and Whitelaw (1969)



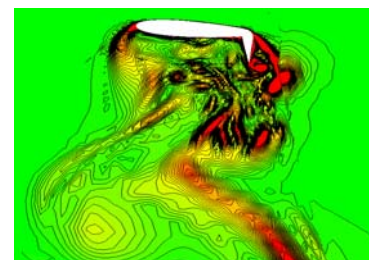
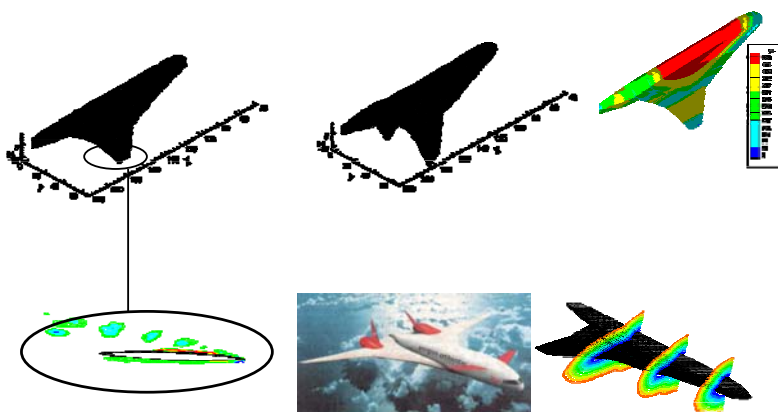
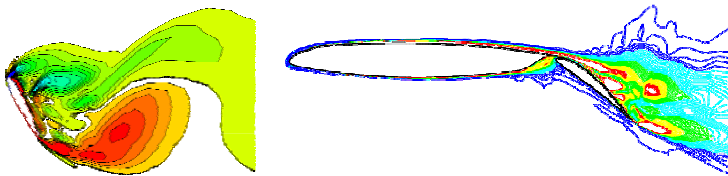
High pressure compressor drum



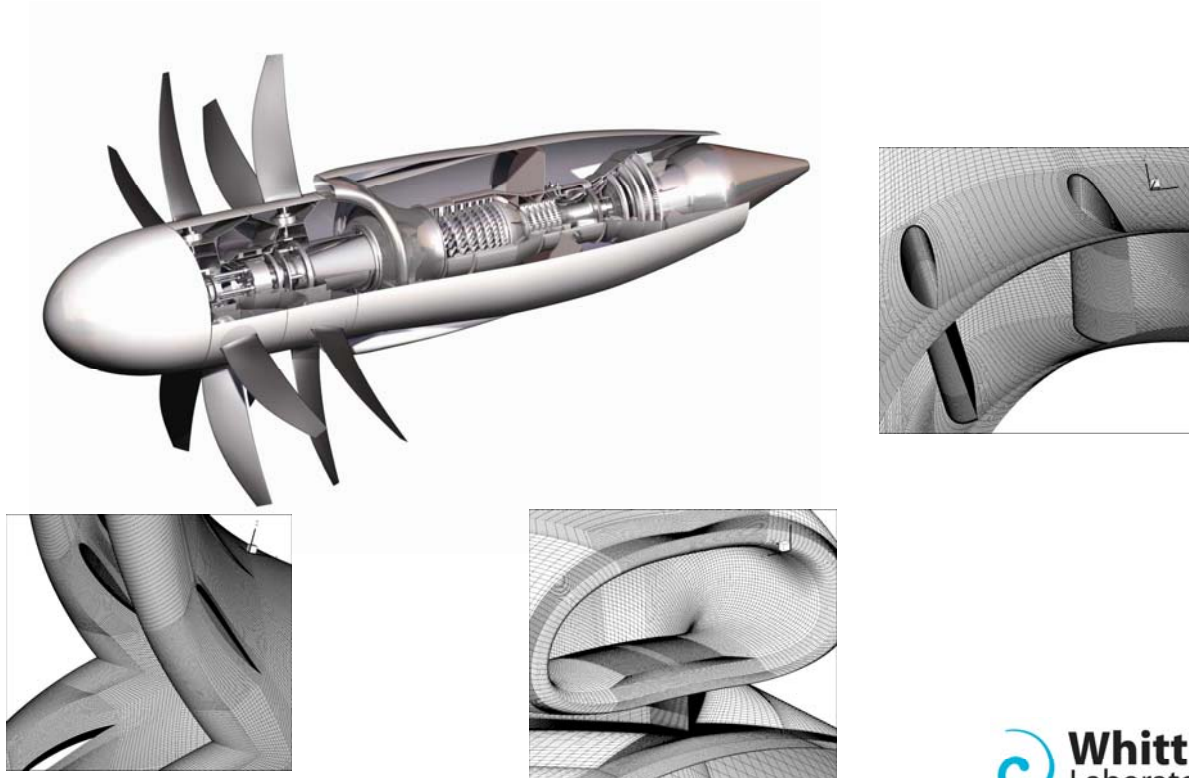
(I)



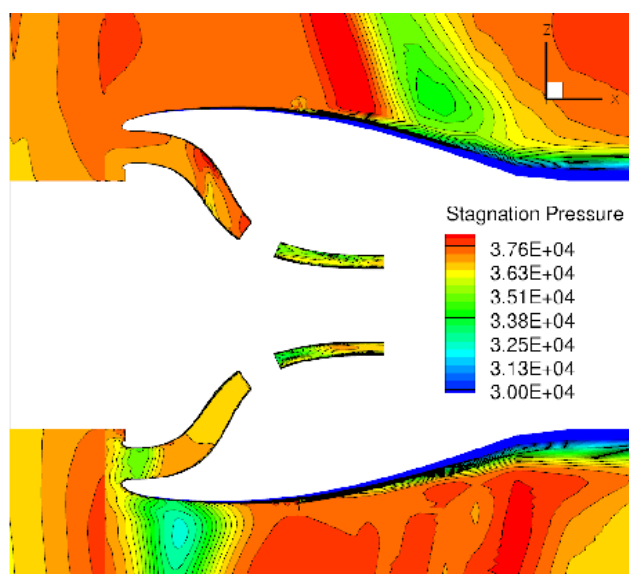
PROBLEM AEROSPACE FLOWS



Open rotor engines



Y0 PLANE



Total Pressure Contours

Experimental data & Best Practices

- To correctly validate/exploit detailed comparisons with $u'u'$ and $E(k)$ data is desirable
- Lacking in many turbomachinery studies
- More importantly LES can need inflow (U, I & Ti) and careful definition of general BCs
- Frequently missing from experimental studies
- To advance LES, both numerical practitioners and experimentalists need to move forward together
- Formal framework for recording simulations and what to record

Conclusions

- High cost of testing and low fidelity of RANS makes the development of LES attractive
- Considered field of 'practical LES', where dissipative RANS based solvers are frequently used
- LES model omission is an attractive option with near wall RANS model – hybrid RANS-NLES
- Combined with suitable grid topologies (hexahedral meshes seem highly preferable) method gives useful results
- For industrial LES hierarchy is: problem definition, wall modeling and grid-solver compatibility with, last of all, the much debated LES model
- Better defined and more detailed validation data and best practice
- Caution must be exercised – still needs user expertise and best practices should be developed